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Precision predictions of pionless EFT and fine tuning in chiral EFT

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In collaboration with: *Hilla De-Leon, Johannes Kirscher, Sergiu Lupu*, Nir Barnea (HUJI). Thanks: Lucas Platter, Bira van Kolck, Francesco Pederiva, Bezalel Bazak, Sebastian König.

Two QCD EFTs

π EFT

- <u>Large scattering length:</u> Nucleons interacting via contact interactions -- Efimov dominates 3-body problem, and power counting
- <u>Origin</u>: low-energy QCD accidentally close to unitarity.
- Very low energies → very light nuclei & low-energy reactions.
- allows a different approach to assess theoretical uncertainty:
 - Renormalizable QFT at LO and NLO – showing cutoff independence, with almost no power counting issues
 - Can be expanded about different momenta – few variations of the EFT
 - Few LECs, i.e., [★]EFT is not a statistical optimization problem.



χΕFT

- <u>Pion dominated theory:</u> Nucleons interacting via pion exchanges and contacts.
- <u>Origin</u>: Standard Model broken chiral symmetry SU(2)_RxSU(2)_L
- Wide range of applications.
- <u>A main challenge</u>:

multivariable systematic uncertainty quantifications in a non-renormalizable theory:

- Statistical optimization
- Bayesian
- Order by order





February 24, 2016

a) Can we learn something useful from π EFT and apply it to χ EFT?

Lupu, Barnea, DG, arXiv: arXiv: 1508.05654

b) Can one observe regulator/space dependence in π EFT, as in χ EFT?

Kirscher, DG, Phys Lett B **755**, 253 (2016)

c) Use π EFT to calculate reactions and compare with χ EFT, to get improved uncertainty estimate: **first** π **EFT calculation of** ³**H beta decay** (@NLO), and a precision calculation of **proton-proton fusion in the Sun**.

De-Leon, DG, in prep., see Hilla De-Leon's poster.

d) A very interesting confirmation of Lattice QCD as well as πEFT consistency check:

first # EFT calculation of ³H, ³He, ²H magnetic moments and n+p \rightarrow d+ γ (@NLO), and comparison to the NPLQCD calculation of 2 nucleons in a magnetic field (Beane et al PRL 115, 132001 (2015))

De-Leon, DG, in prep..





 χ π EFT and χ EFT are both EFTs of the nuclear regime at low energy

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πEFT @ LO

Bedaque, Hammer, van-Kolck: (1999) triton B.E. at LO has strong cutoff dependence \rightarrow add 3-body contact at LO







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6

$\hbar \pi EFT$ – and Correlations in light nuclei

- No 4 body parameter at LO.
- One 3b force one line!
- Tjon/Phillips correlation originate in Efimov physics.



Platter (2006), Platter, Hammer, Meissner (2005), Kirscher, Griesshammer, Hofmann (2007)

Nogga, Bogner, Schwenk (2005)

χ 2 EFT – three body problem in the (c_D, c_E) plane.



Lupu, Barnea, DG, arXiv: arXiv: 1508.05654

χ EFT – a Tjon line representation



Lupu, Barnea, DG, arXiv: arXiv: 1508.05654

8

χ EFT – a Tjon line representation



Lupu, Barnea, DG, arXiv: arXiv: 1508.05654

9

χ EFT – a Tjon line representation



Lupu, Barnea, DG, arXiv: arXiv: 1508.05654

χ EFT – RG evolved potential



χ EFT – RG evolved potential



$\star \chi EFT - RG$ evolved potential



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χ EFT – RG evolved potential



15

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 A=3 Efimov effect: triton at LO has strong cutoff dependence →add 3-body contact at LO.



³H: Schrödinger formalism, local regulator

- We have utilized a Schrödinger formalism for pionless EFT, with the same counting scheme.
- Cutoff potentials using local gaussian regulators (*a-la* local- χ EFT).
- LO potential is iterated using the Schrödinger equation.
- NLO is treated perturbatively, using first order perturbation theory, which is found to be identical to the distorted wave born approximation.



³H: Schrödinger formalism, local regulator



19

J. Kirscher, D. Gazit, PLB **755**, 253 (2016)

\times ³He: one more difference between the two approaches



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Compare with König et al (2011, 2013, 2014, 2015) in the dibaryon QFT formalism:

- -- order of magnitude smaller cutoff dependence for non-pert. Coulomb calculation
- -- Similar results in the perturbative Coulomb case.

Kong, Ravndal (1999,2001), Rupak, Kong (2003), Ando, Birse (2010)

⁴He – preliminary results@LO (no coulomb)



21



J. Kirscher et al, preliminary

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\checkmark Weak proton-proton fusion in the Sun

SFII – Adelberger et al., Rev. Mod. Phys. 83, 195 (2011)



- Cannot be measured terrestrially depends on theory
 Very low proton-proton relative momentum (*E_{rel}~6 keV*).
 - Needed accuracy: ~1%.

$$\sigma(E) = \frac{S(E)}{E} \exp[-2\pi\eta(E)]$$

$$E) = S(0) + S'(0)E + S''(0)E^2/2 + \cdots$$



Veak proton-proton fusion in the Sun – theory standards

SFII – Adelberger et al., Rev. Mod. Phys. 83, 195 (2011)

 $3.99(1 \pm 0.030) \times 10^{-25}$ MeV b pionless EFT.

SFII recommended value (2011): $S_{11}(0) = 4.01(1 \pm 0.009) \times 10^{-25}$ MeV b.

<u>Modern χ EFT calculation by Marcucci et al., Phys. Rev. Lett. (2013)</u>: Use consistent ³H decay-rate to constrain consistently axial MEC (DG, Quaglioni, Navratil, PRL 2009), and predict pp-fusion rate.

$$S(0) = (4.030 \pm 0.006) \times 10^{-23} \text{ MeV fm}^2$$

Including: p-wave contribution (+0.005%), full EM (-0.0025-(-0.0075)%), difference between 500 and 600 MeV cutoff and potential models.





Precision, Uncertainty, and predictions



Advantages of *π*EFT UQ for proton-proton fusion:1. Small number of parameters.

- 2. Two π EFT expansions.
- 3. A "cheat-sheet" in the electromagnetic sector.
- 4. Cutoff independence up to infinity.

We revisit the pp-fusion problem within pionless EFT, fixing the unknown LEC using triton decay.



A fully perturbative pionless EFT A=2, 3 calculation @NLO

- LO Parameters:
 - nn and 2-np Scattering lengths: ³S₁, ¹S₀.
 - pp scattering length.
 - Fine structure constant.
 - Three body force strength to prevent Thomas collapse.
- NLO parameters:
 - 2 effective ranges.
 - Renormalizations of pp and 3NF.
 - (isospin dependent 3NF to prevent logarithmic divergence in the binding energy of ³He).
- Weak Interaction: LO (g_A 1 body), NLO (L_{1A} 2 body)
- EM Interaction: LO $(\kappa_s, \kappa_v) 1$ body), NLO $(L_1, L_2 2$ body)



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The role of the deuteron tail

- Many low energy reactions depend on deuteron normalization.
- One has a choice of constructing pionless EFT:



Both theories are valid EFTs. Z-parameterization sometimes has quicker convergence.

> Phillips, Rupak, Savage, Phys. Lett. **B473**, 209 (2000) Grießhammer, Nucl. Phys. **A744**, 192 (2004)

29



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Analogy between weak and EM:

	5
EM	weak
κ_n, κ_p	g A
σ , σau^0	$\sigma au^{+,-}$, $ au^{+,-}$
$L_1(d^i)^\dagger s^j$, $L_2(d^i)^\dagger d^j$	$L_{1A}(d^i)^\dagger s^j$
$\sigma_{np}: n+p \rightarrow d+\gamma$	<i>pp</i> fusion:
d magnetic moment $\langle \mu_{d} angle$	$p+p ightarrow d+e^++ u_e$
³ H, ³ He magnetic moments:	³ H β -decay into ³ He:
$\langle \mu_{^3 ext{H}} angle$, $\langle \mu_{^3 ext{He}} angle$	$^{3}\text{H} ightarrow ^{3}\text{He} + e^{-} ar{ u_{e}}$
	EM κ_n, κ_p $\sigma, \sigma \tau^0$ $L_1(d^i)^{\dagger} s^j, L_2(d^i)^{\dagger} d^j$ $\sigma_{np} : n + p \rightarrow d + \gamma$ <i>d</i> magnetic moment $\langle \mu_d \rangle$ ³ H, ³ He magnetic moments: $\langle \mu_{^3H} \rangle, \langle \mu_{^3He} \rangle$

Use the same strategy in both cases: fix probe LECs at A=3 and predict A=2.



Precision, Uncertainty, and predictions



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Adding the NLO 1-body contributions

35



1st estimate of theoretical uncertainty: All NLO contributions are of the same order, one can estimate higher order effects as the NLO contribution.



All NLO contributions are of the same order,

one can estimate higher order effects as the NLO contribution.

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Rho-parameterization

Zed-parameterization

$$ft = \frac{K}{G_F^2 V_{ud}^2 \left[\left| \left\langle {}^3 \mathrm{H} \right| \right| \mathcal{V}_{\mu}^{+} \right| {}^3 \mathrm{He} \right\rangle \right|^2 + \frac{f_A}{f_V} \left| \left\langle {}^3 \mathrm{H} \right| \left| \mathcal{A}_{\mu}^{+} \right| {}^3 \mathrm{He} \right\rangle \right|^2 \right]}$$



 $4.02 \cdot 10^{-23} \text{MeV} \cdot fm^{2} \pm 0.01$ $3.90 \cdot 10^{-23} \text{MeV} \cdot fm^{2}$ $4.16 \cdot 10^{-23} \text{MeV} \cdot fm^{2}$ $\overset{-}{_{2}}_{5 \ 10^{3} \ 2}_{5 \ 10^{4} \ 2}_{5 \ 10^{5} \ 2}_{5 \ 10^{5} \ 2}_{5 \ 10^{6} \ 2}_{5 \ 10^{7}}_{5 \ 10^{7}}$

Translates to $\pm 2\%$ difference in pp fusion

1st estimate of theoretical uncertainty: All NLO contributions are of the same order, one can estimate higher order effects as the NLO contribution.



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In the EM sector:



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39

Capture reaction $(n+p \rightarrow d+\gamma)$ depends stronger on deuteron tail, same order of theoretical uncertainty again (a few percents).

In the EM sector:

PRL 115, 132001 (2015)

PHYSICAL REVIEW LETTERS

week ending 25 SEPTEMBER 2015

Ab initio Calculation of the $np \rightarrow d\gamma$ Radiative Capture Process

Silas R. Beane,¹ Emmanuel Chang,² William Detmold,³ Kostas Orginos,^{4,5} Assumpta Parreño,⁶ Martin J. Savage,² and Brian C. Tiburzi^{7,8,9}

(NPLQCD Collaboration)



Our prediction for l_1 =-3.3-(-5.7) fm



So... is 3% too big to be called precision physics?





So... is 3% too big to be called precision physics?

g_A systematic uncertainty



i.e., theoretical uncertainty (3%) of the same order of systematic experimental error encapsulated in g_A and ³H half life (2% total).



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Summary

We can learn something useful from #EFT and apply it to χEFT – disregarding correlations from #EFT would result in fine tuning!
 One should augment covariance matrices.

Lupu, Barnea, DG, arXiv: arXiv: 1508.05654

b) One observes regulator/space dependence in π EFT just as in χ EFT.

Kirscher, DG, Phys Lett B 755, 253 (2016), Kirscher et al, in prep.

c) First #EFT calculation of ³H beta decay (@NLO), and a precision calculation of proton-proton fusion in the Sun:

Improved and reliable theoretical uncertainty estimate. Improvement in g_A and ³H decay determination highly needed. N2LO calculation should follow.

What can this do for SSM? A lot, mainly to CNO neutrinos flux

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d) A very interesting confirmation of Lattice QCD as well as #EFT consistency check: first #EFT calculation of ³H, ³He, ²H magnetic moments and n+p→d+γ (@NLO), and good comparison to the NPLQCD calculation of 2 nucleons in a magnetic field (Beane et al PRL 115, 132001 (2015))

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