

Chiral Nuclear Forces at N⁴LO

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Outline

- **Introduction**
- **Some misconceptions concerning (chiral) nuclear forces**
- **What's next? The chiral expansion at N4LO**
- **Outlook**

History and current status of chiral nuclear forces

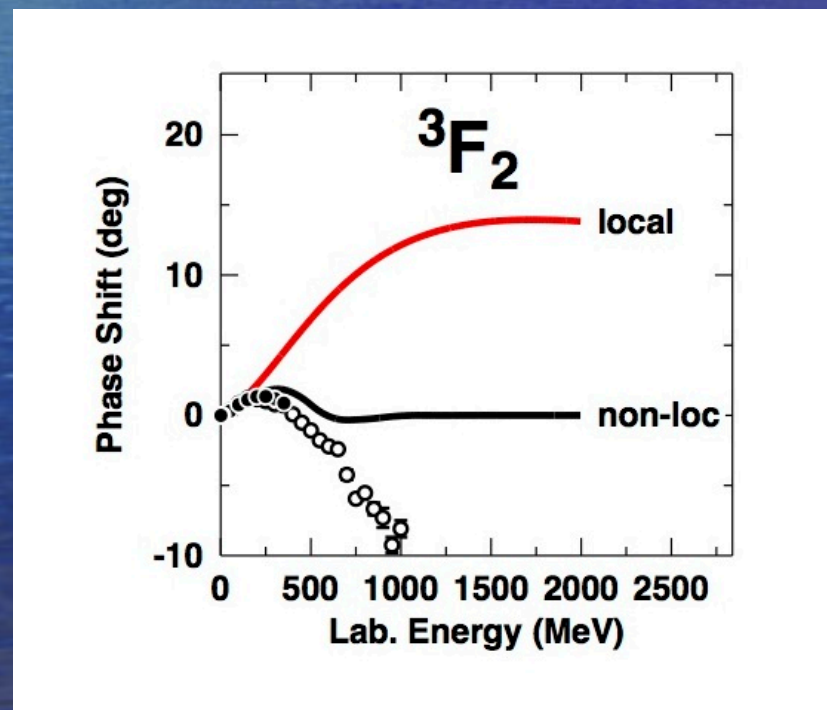
- Since 20+ years, the idea of using chiral EFT for the derivation of nuclear forces is around (Weinberg, van Kolck). The ideas are by now well-known in this community, and I will not repeat them.
- Since 10+ years, quantitative chiral NN potentials exist up to N3LO.
- With these potentials (+chiral 3NFs), numerous exact few-body and *ab initio* many-body calculations have been performed---with some success. But there are also unsolved problems.
- **What are the reasons for the open problems?**
- **The current nuclear forces may be still deficient.**
- **Thus, the current research on nuclear forces is characterized by attempts to improve those forces.**
- **Let's look at the facts and address some common misconceptions.**

Myth #1: Local cutoffs are better than non-local ones.

Wrong!

Why?

- Potentials with local cutoffs never go to zero on-shell and, thus, the phase shifts grow forever.



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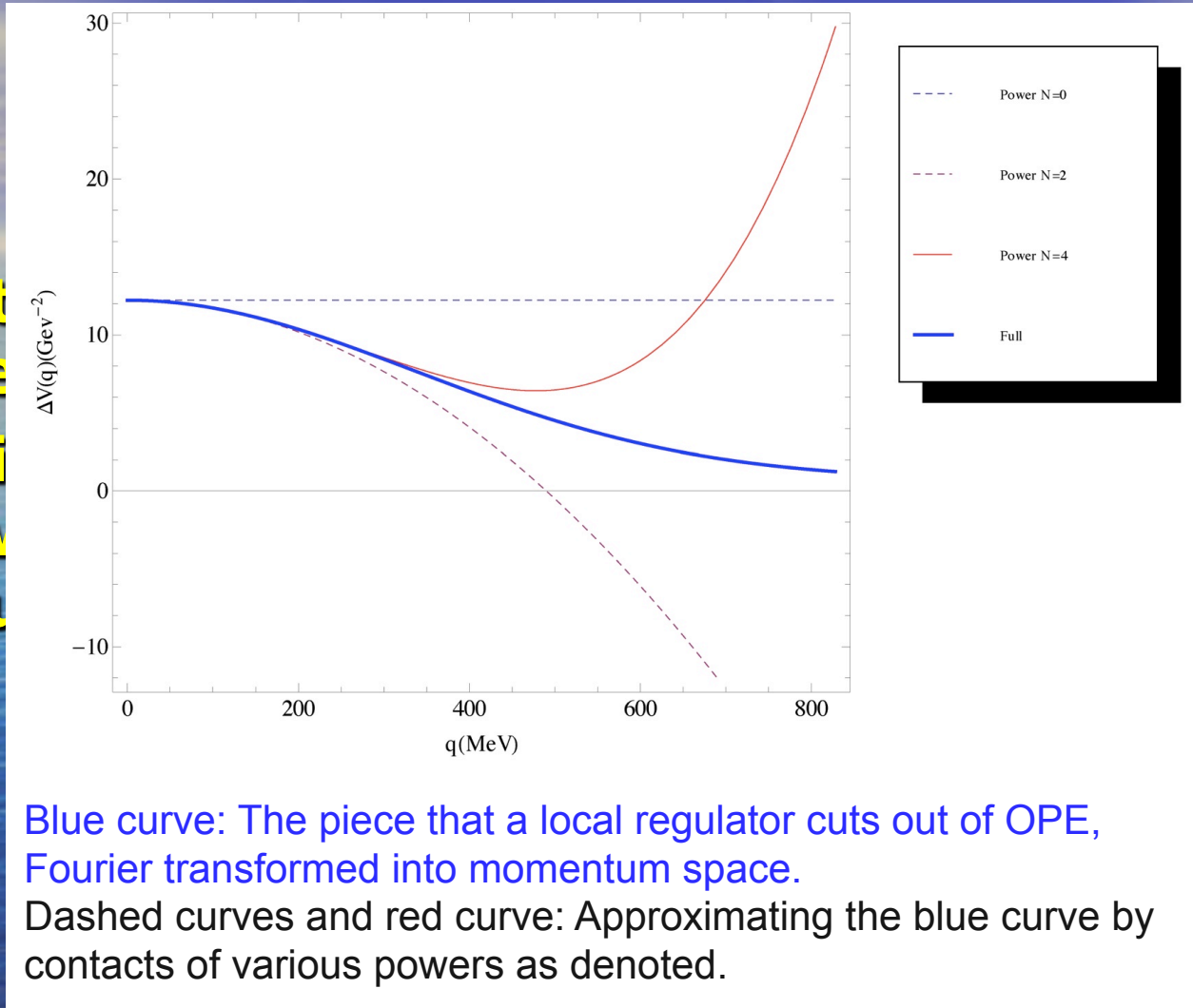
Why?

- Potentials with local cutoffs never go to zero on-shell and, thus, the phase shifts grow forever.
- Chiral EFT is an expansion in momenta. What power in momentum is the local cutoff function equivalent to?

$$f\left(\frac{r}{R}\right) = \left[1 - \exp\left(-\frac{r^2}{R^2}\right)\right]^n$$

Myth #1: Local cutoffs are better than non-local ones.

- Potentials
- Shell
- Chiral perturbation theory
- Equations



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- **Inconsistent with proper power counting!**

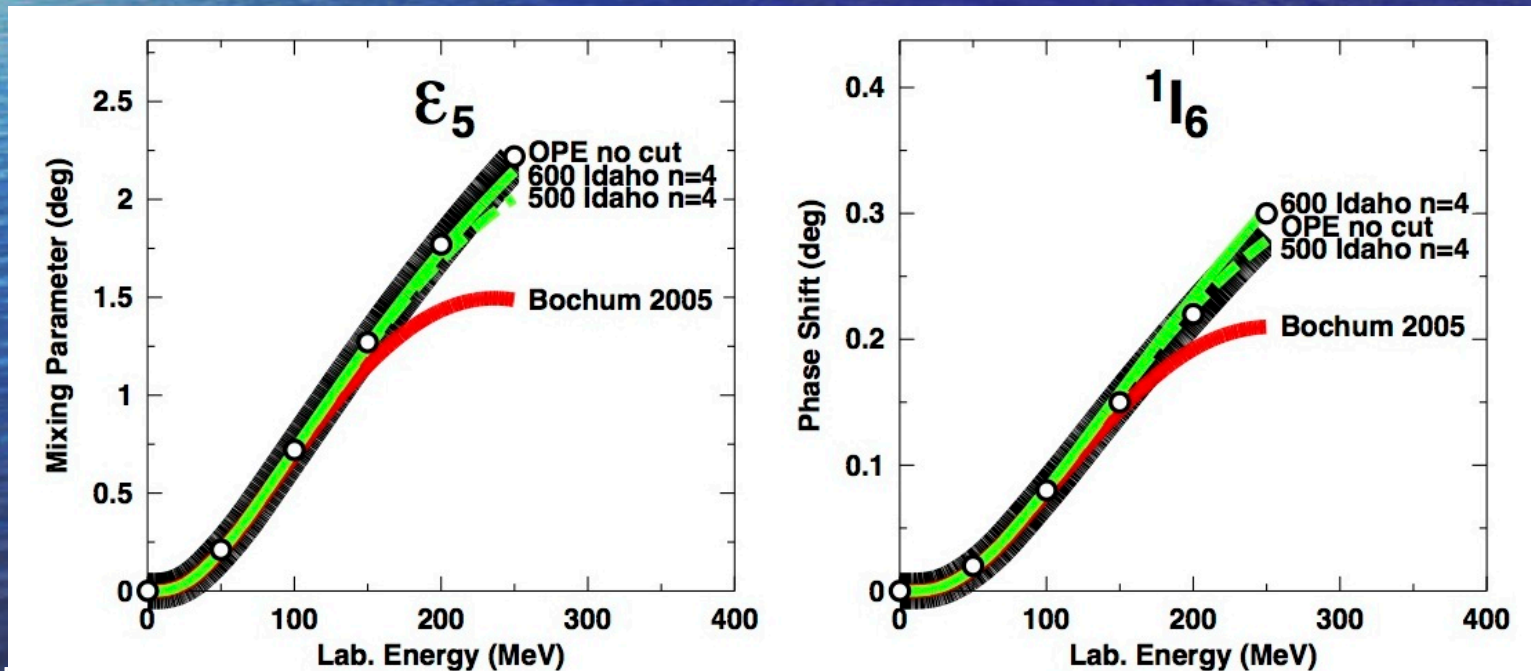
Myth #2: Non-local cutoffs are cutting down the long-range part too much.

Wrong!

Why?

- It depends on the power of the non-local regulator:

$$f(p', p) = \exp[-(p'/\Lambda)^{2n} - (p/\Lambda)^{2n}]$$



Myth #3: When local cutoffs are used in the 3NF then, consistency requires, that local cutoffs are also used in the 2NF .

Wrong! **Why?**

- **Cutoffs generate powers of momenta beyond the given order; the coefficients don't matter (as long as they are natural). Local vs. non-local differ only by those coefficients:**

$$\begin{aligned} f_{\text{nonlocal}}(p', p) &= \exp[-(p'/\Lambda)^{2n} - (p/\Lambda)^{2n}] \\ &\approx 1 - \left[\left(\frac{p'}{\Lambda}\right)^{2n} + \left(\frac{p}{\Lambda}\right)^{2n} \right] + \frac{1}{2} \left[\left(\frac{p'}{\Lambda}\right)^{2n} + \left(\frac{p}{\Lambda}\right)^{2n} \right]^2 - + \dots \\ f_{\text{local}}(q) &= \exp[-(\vec{q}/\Lambda)^{2n}] \\ &\approx 1 - \left[\left(\frac{p'}{\Lambda}\right)^2 + \left(\frac{p}{\Lambda}\right)^2 - 2 \frac{\vec{p}' \cdot \vec{p}}{\Lambda^2} \right]^n + \frac{1}{2} \left[\left(\frac{p'}{\Lambda}\right)^2 + \left(\frac{p}{\Lambda}\right)^2 - 2 \frac{\vec{p}' \cdot \vec{p}}{\Lambda^2} \right]^{2n} - + \dots \end{aligned}$$

with $\vec{q} = \vec{p}' - \vec{p}$, the momentum transfer; $q = |\vec{q}|$.

Myth #4: For 3NFs, local cutoffs are better than non-local ones.

Wrong!

Why?

- **Both are equally good or bad. Use what works best for you.**
- **In the NCSM, locals seem to work better (Navratil, FBS 41, 117 (2007)).**
- **In CC calculations of nuclear matter, locals showed bad convergence (Hagen et al., PRC 89, 014319 (2014)).**

Myth #5: Fitting phase shifts (and not data) is good enough for a high-precision potential.

Wrong!

Why?

- As pointed out correctly by the Nijmegen group some 20 years ago, phase shift χ^2 can be very misleading concerning the true reproduction of the NN data.

- **Example:**

Neutron-proton χ^2 /datum 0-200 MeV

	Idaho N3LO 500	Idaho N3LO 600	Bochum N3LO 550/600
Using data	1.1	1.2	1.3
Using phase shifts	2.2	5.3	2.1

Myth #6: Fitting a NN potential to just one NN data set is sufficient to demonstrate “high precision”.

Wrong!

Why?

- **Even the craziest NN potential can fit one data set.**
- **The point is to fit all 5000+ NN data.**

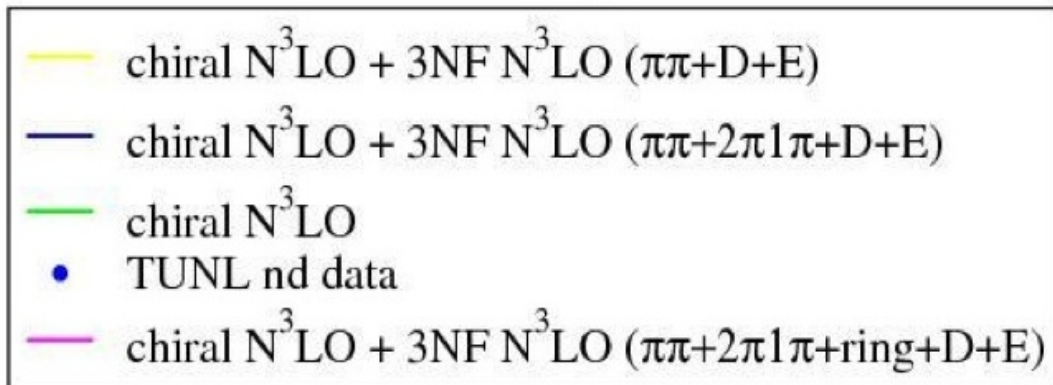
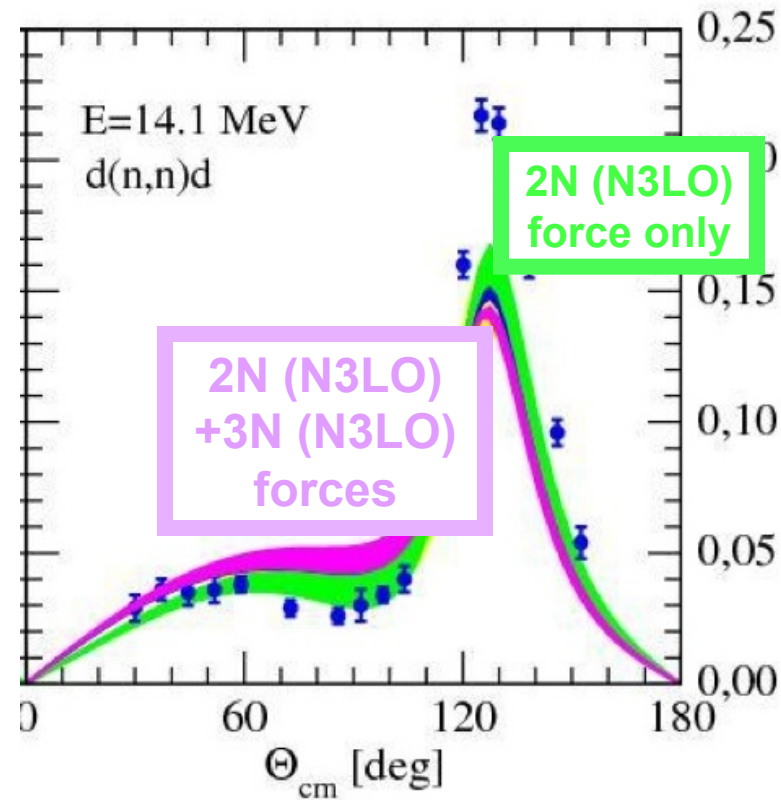
Now that we know what **NOT** to do.

What should we do?

Evaluate current status. Anything left to do in the nuclear force business?

- **Current status: 2NFs and 3NFs up to N3LO are applied in nuclear few- and many-body systems.**
- **In general, quite a bit of success, but some persistent problems remain.**
- **In the few-body sector: A_y puzzle, N-d break-up, ...**

N-d A_y calculations by Witala et al.

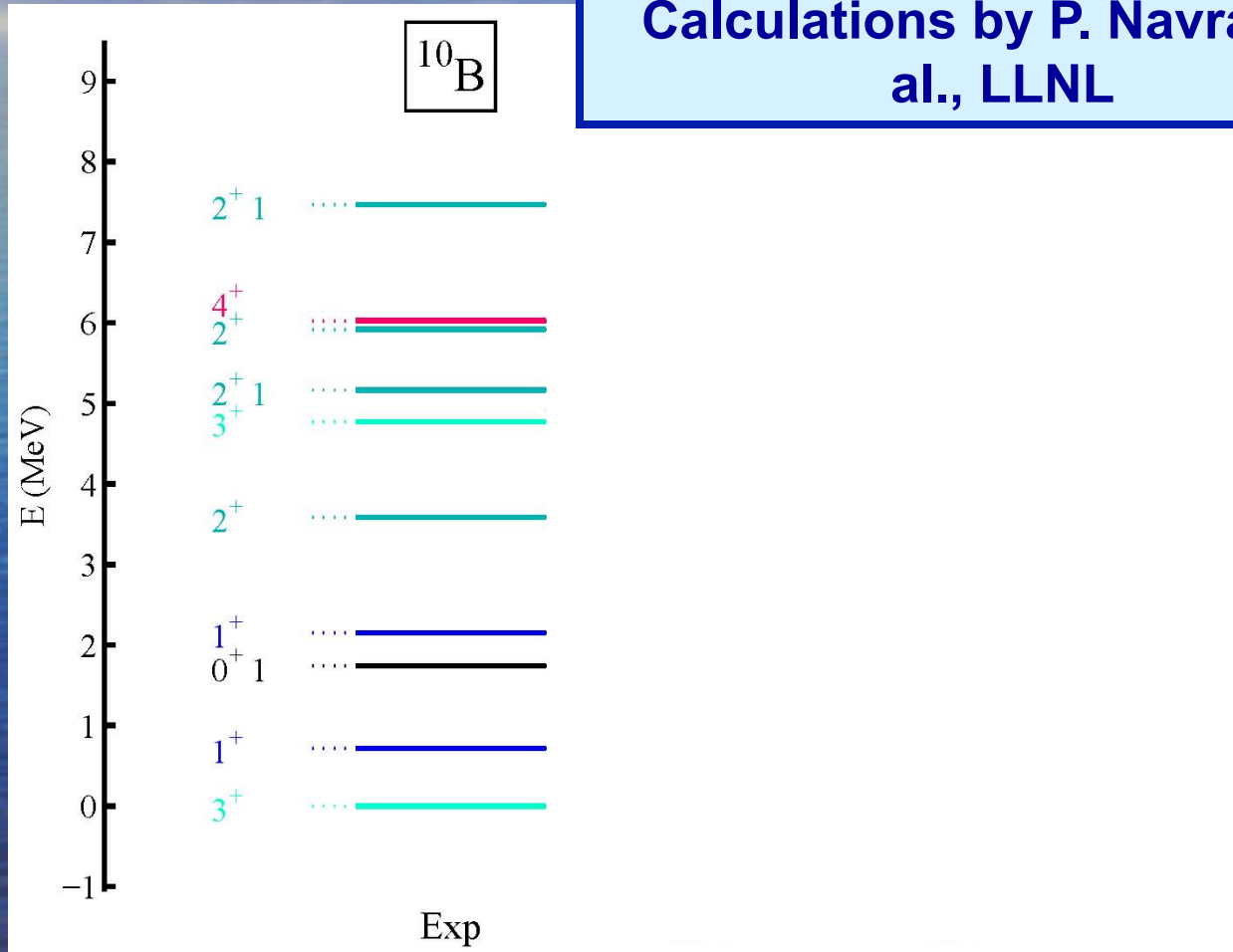


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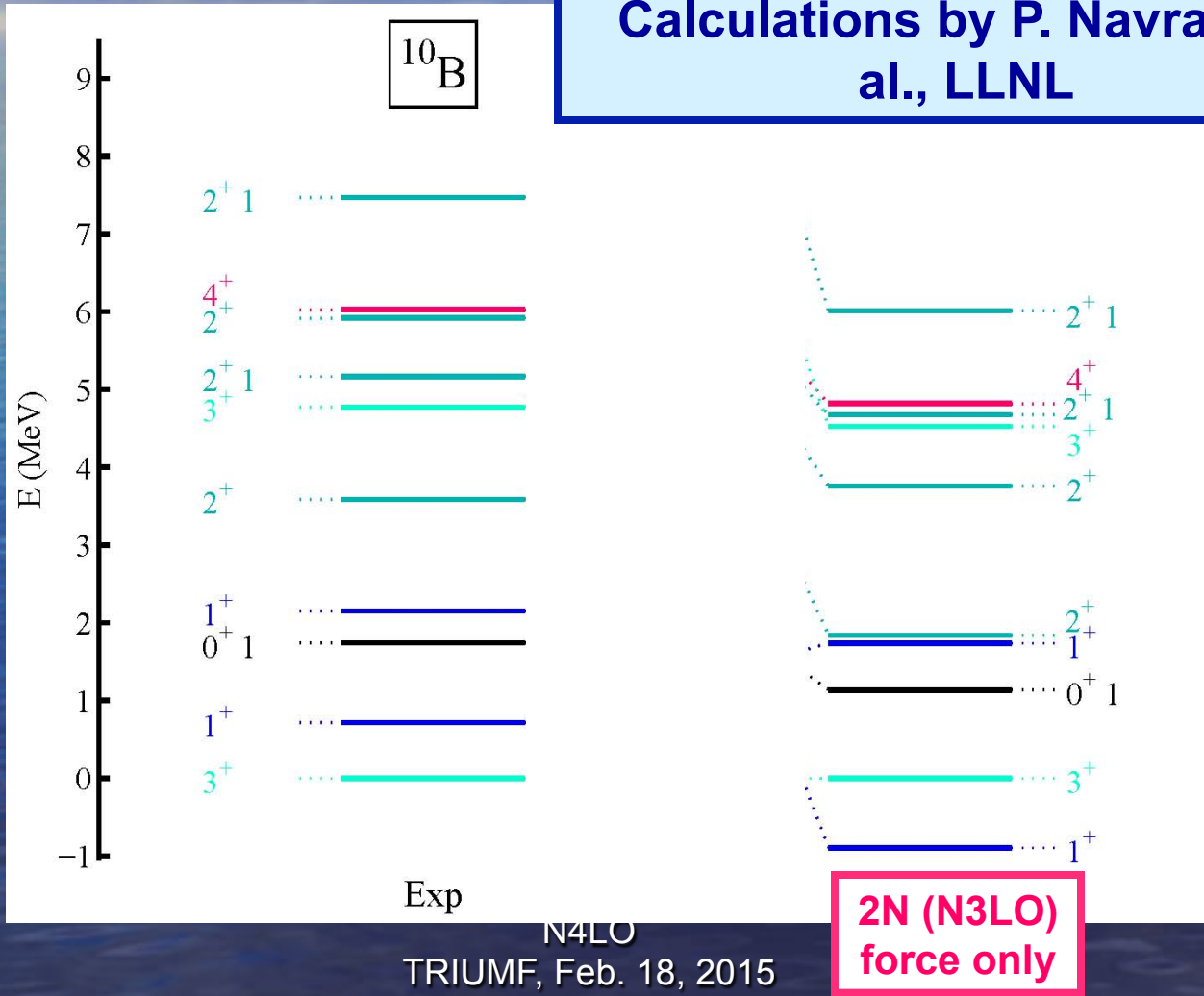
Calculating the properties of **light nuclei** using chiral 2N and 3N forces

“No-Core Shell Model”
Calculations by P. Navratil et al., LLNL



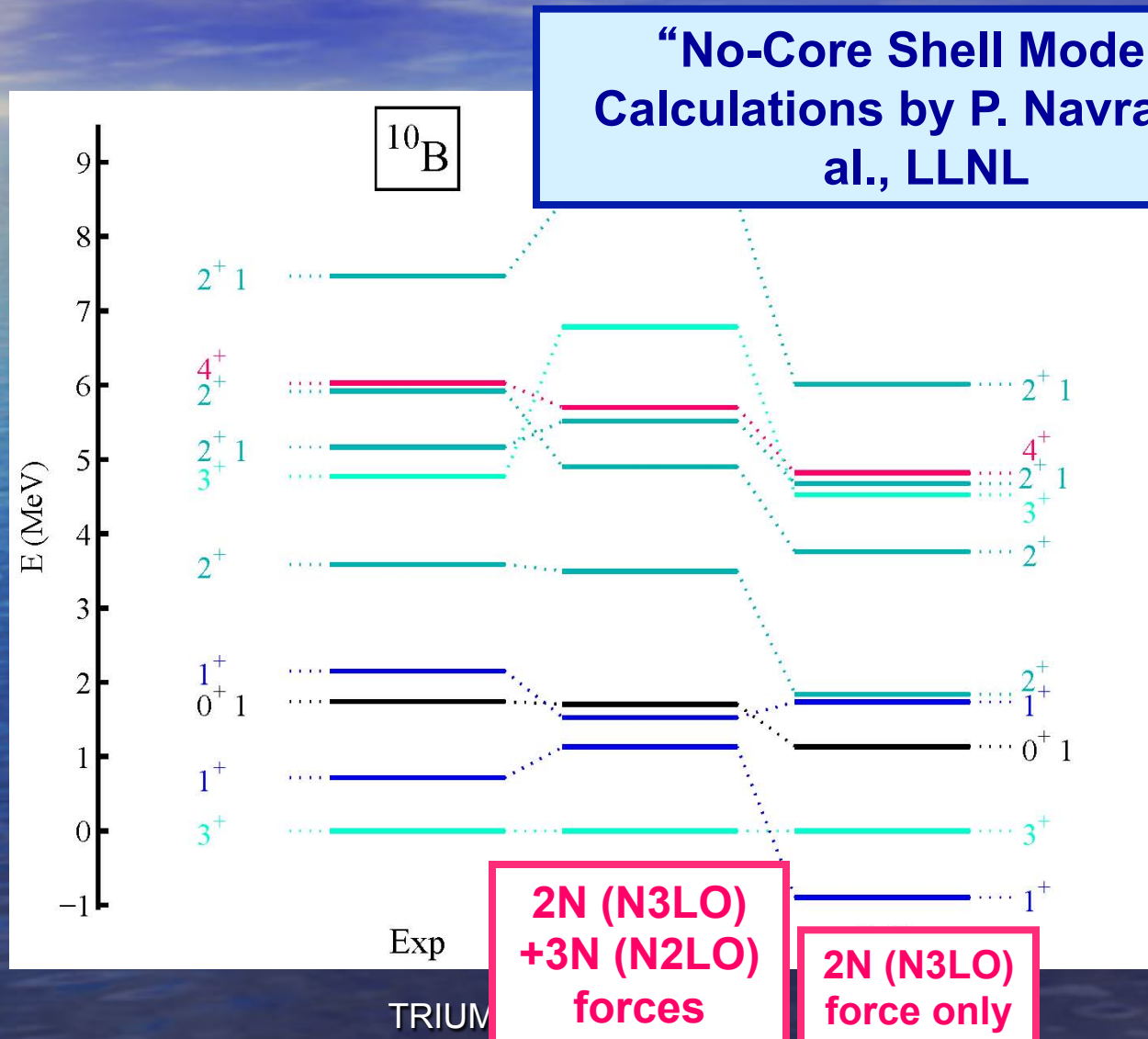
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2N (N3LO)
force only

Calculating the properties of light nuclei using chiral 2N and 3N forces



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- **Intermediate nuclei: Overbinding.**

Ground-state energies from O-16 to Sn-132 obtained in CC with 2NF + 3NF

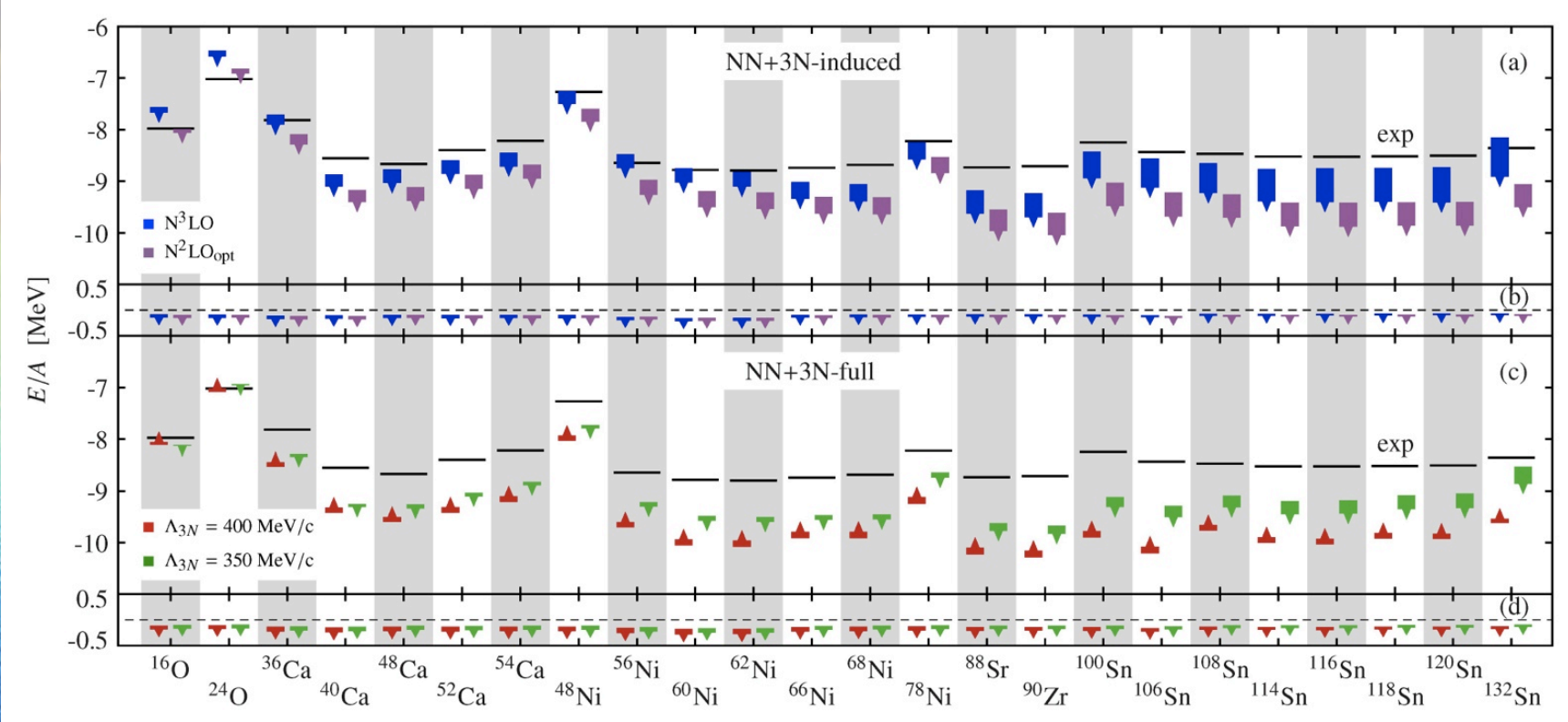


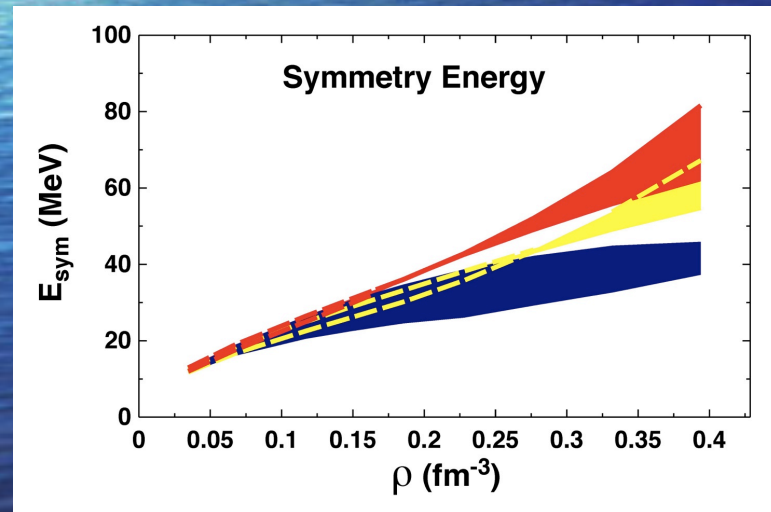
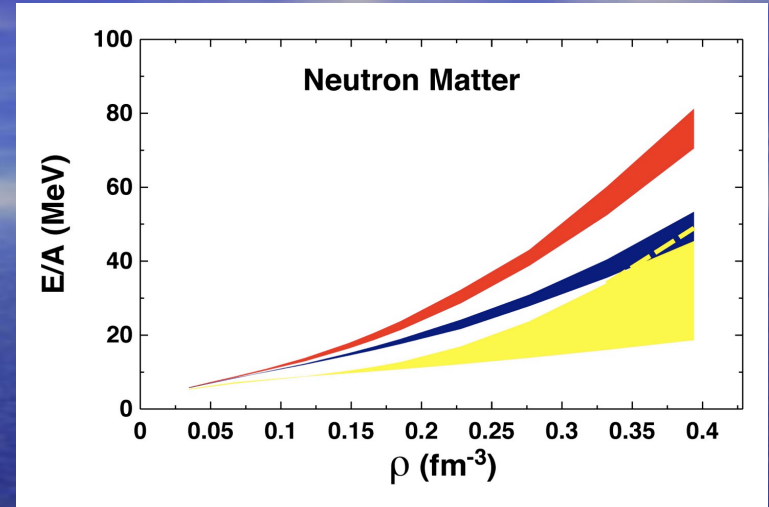
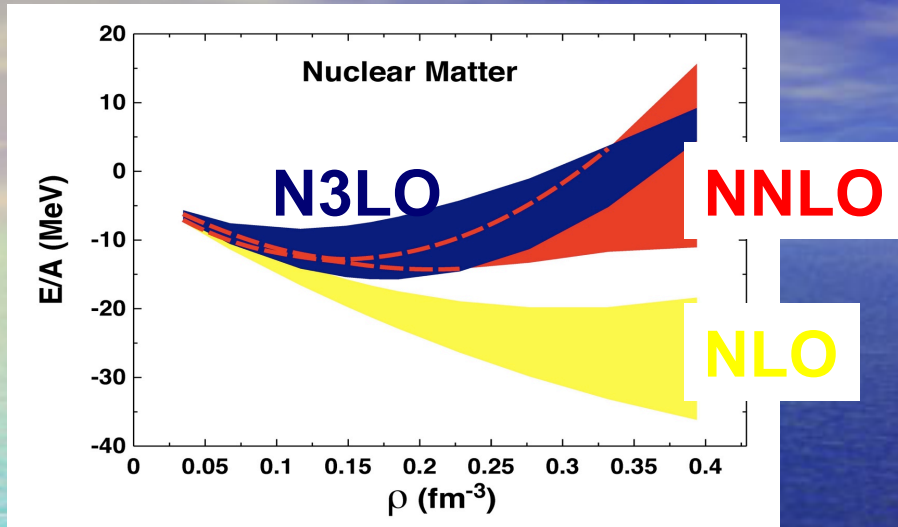
FIG. 5: (Color online) Ground-state energies from CR-CC(2,3) for (a) the $NN+3N$ -induced Hamiltonian starting from the N^3LO and N^2LO_{opt} optimized NN interaction and (c) the $NN+3N$ -full Hamiltonian with $\Lambda_{3N} = 400$ MeV/c and $\Lambda_{3N} = 350$ MeV/c. The boxes represent the spread of the results from $\alpha = 0.04$ fm⁴ to $\alpha = 0.08$ fm⁴, and the tip points into the direction of smaller values of α . Also shown are the contributions of the CR-CC(2,3) triples correction to the (b) $NN+3N$ -induced and (d) $NN+3N$ -full results. All results employ $\hbar\Omega = 24$ MeV and 3N interactions with $E_{3max} = 18$ in NO2B approximation and full inclusion of the 3N interaction in CCSD up to $E_{3max} = 12$. Experimental binding energies [32] are shown as black bars.

From S. Binder et al., PLB 736, 119 (2014).

Evaluate current status. Anything left to do in the nuclear force business?

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- **In the few-body sector: A_y puzzle, N-d break-up, ...**
- **Light nuclei: Spectra not perfect.**
- **Intermediate nuclei: Overbinding.**
- **Convergence of the chiral expansion in the many-body system?**

Order-by-order convergence ???



From
F. Sammarruca et al.,
arXiv:1411.0136.

N4LO

Evaluate current status. Anything left to do in the nuclear force business?

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- **In general, quite a bit of success, but some persistent problems remain.**
- **In the few-body sector: A_y puzzle, N-d break-up, ...**
- **Light nuclei: Spectra not perfect.**
- **Intermediate nuclei: Overbinding.**
- **Convergence of the chiral expansion in the many-body system? **Not converged at N3LO.****

Because of the problems just demonstrated, improvement of current nuclear forces is called for

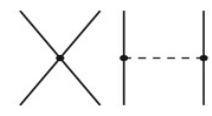
- **How?**
- **Go to next order!**
- **That is: Turn to N4LO.**
- **What can we expect from N4LO?**
- **Does N4LO have anything to offer we were not offered before?**

2N Force

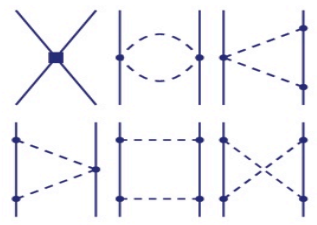
3N Force

4N Force

LO
 $(Q/\Lambda_\chi)^0$



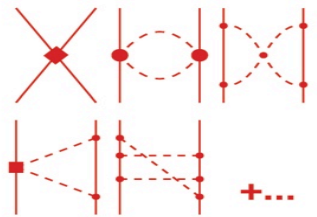
NLO
 $(Q/\Lambda_\chi)^2$



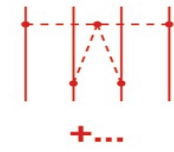
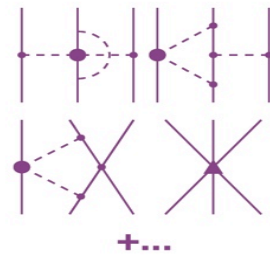
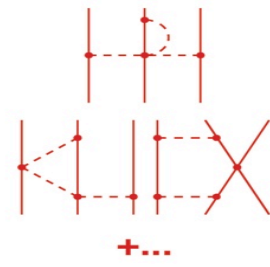
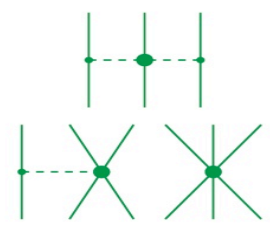
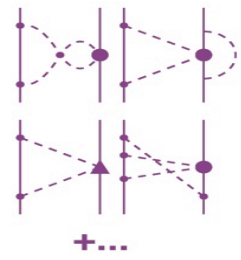
NNLO
 $(Q/\Lambda_\chi)^3$



N³LO
 $(Q/\Lambda_\chi)^4$



N⁴LO
 $(Q/\Lambda_\chi)^5$

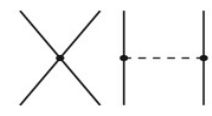


2N Force

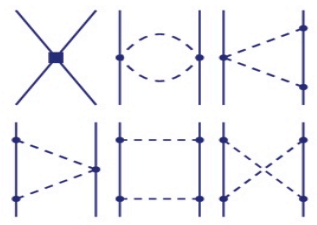
3N Force

4N Force

LO
 $(Q/\Lambda_\chi)^0$



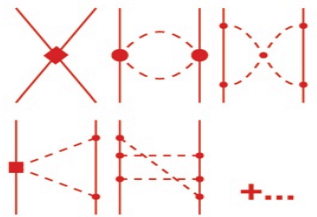
NLO
 $(Q/\Lambda_\chi)^2$



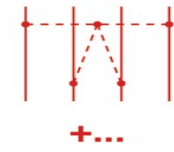
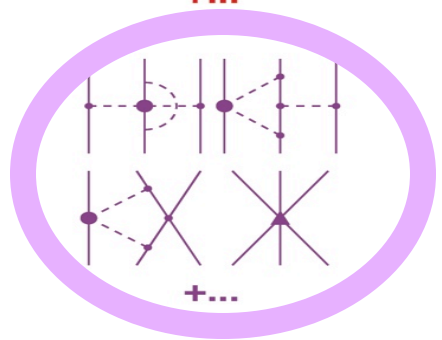
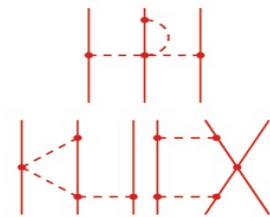
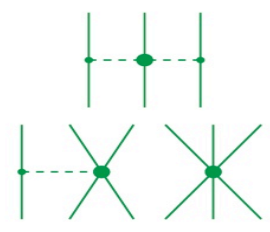
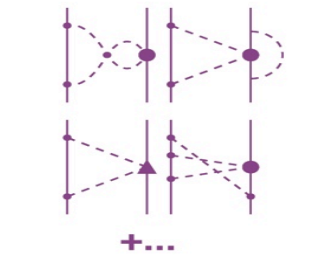
NNLO
 $(Q/\Lambda_\chi)^3$

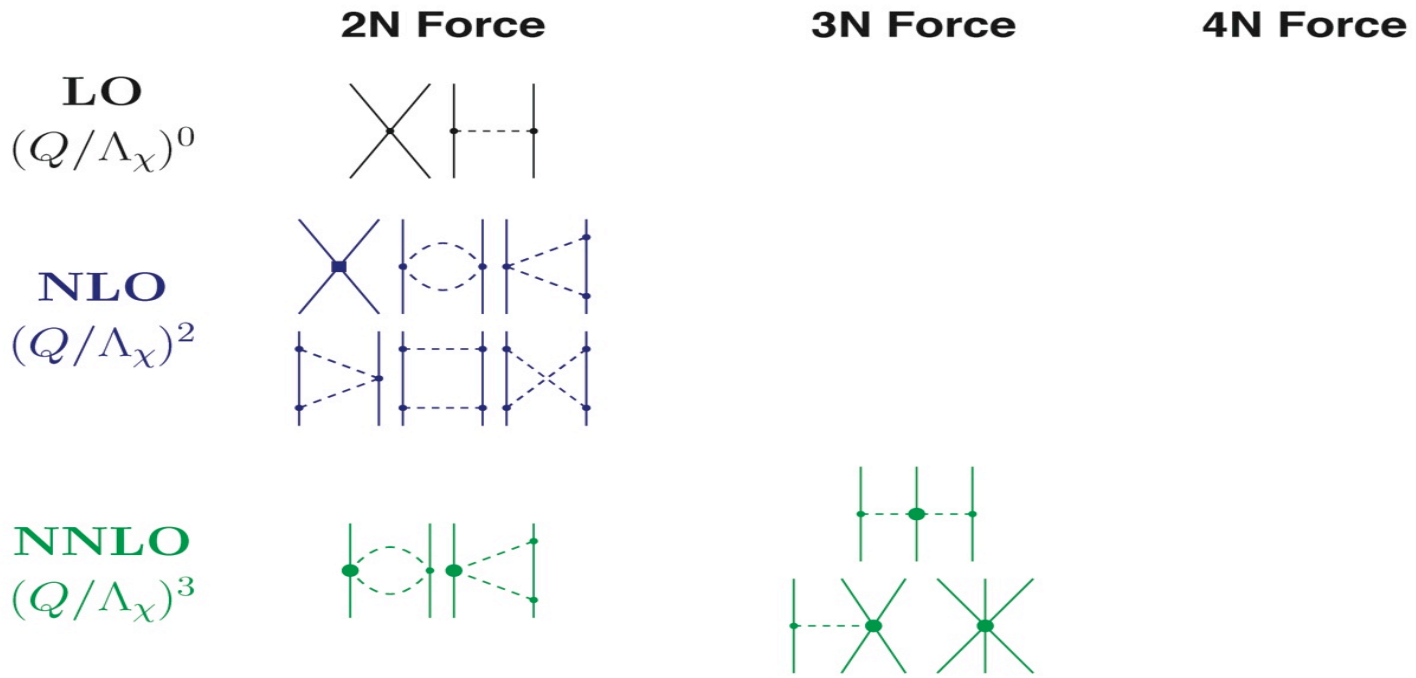


N³LO
 $(Q/\Lambda_\chi)^4$



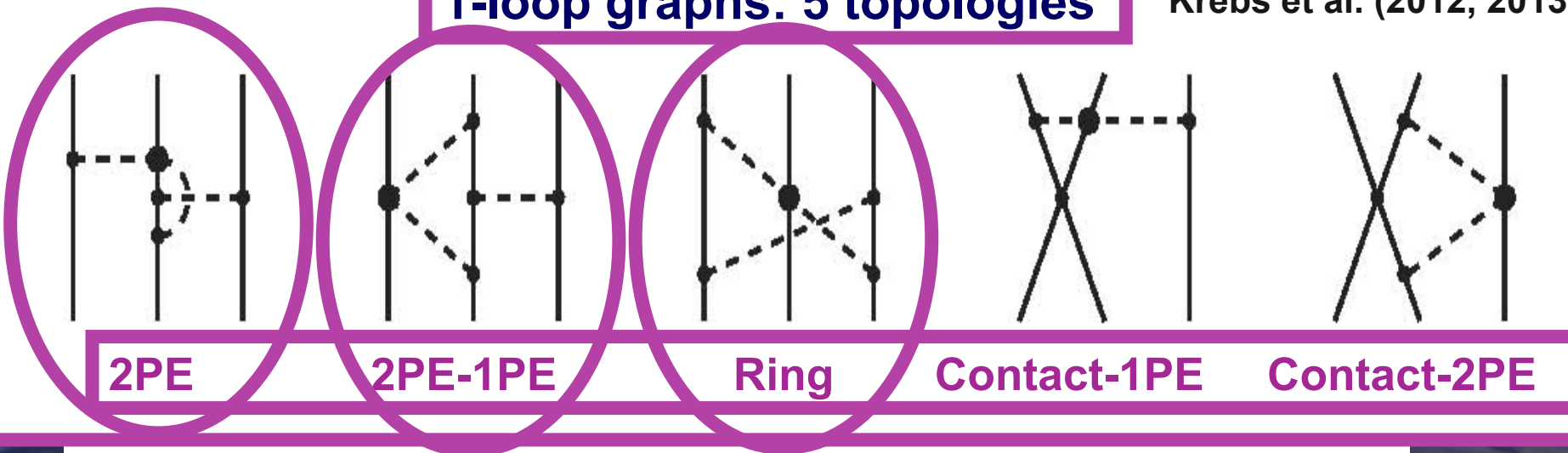
N⁴LO
 $(Q/\Lambda_\chi)^5$





1-loop graphs: 5 topologies

Krebs et al. (2012, 2013)

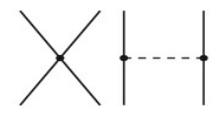


2N Force

3N Force

4N Force

LO
 $(Q/\Lambda_\chi)^0$

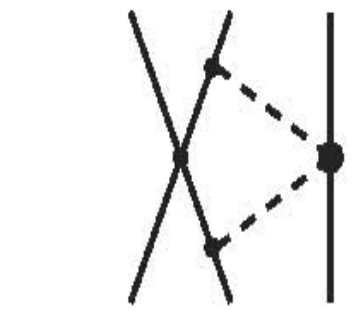
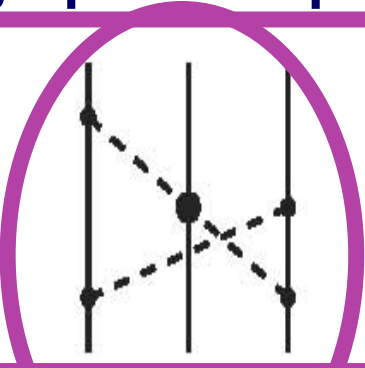
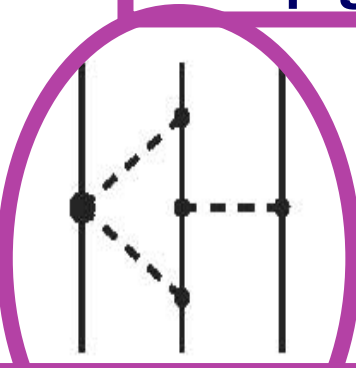
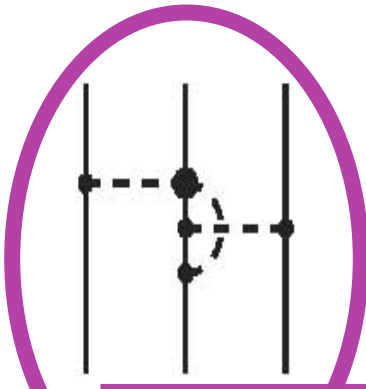


NLO
 $(Q/\Lambda_\chi)^2$



1-loop graphs: 5 topologies

Krebs et al. (2012, 2013)



2PE

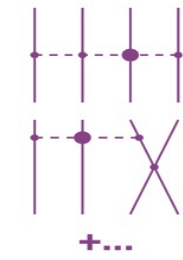
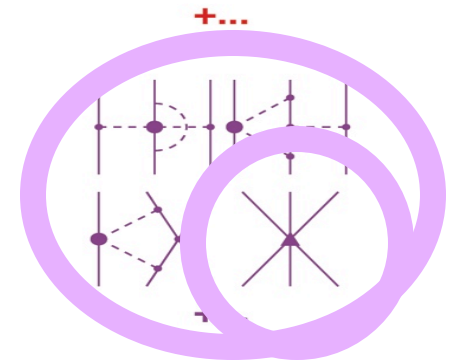
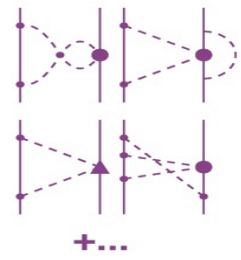
2PE-1PE

Ring

Contact-1PE

Contact-2PE

N⁴LO
 $(Q/\Lambda_\chi)^5$



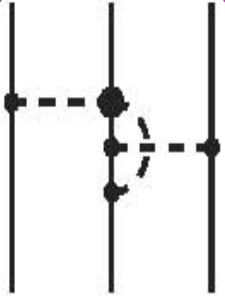
2N Force

3N Force

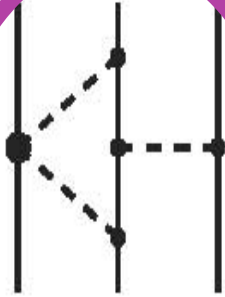
4N Force

1-loop graphs: 5 topologies

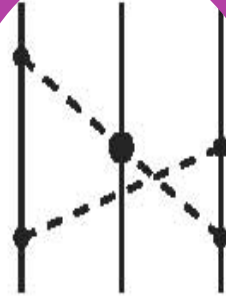
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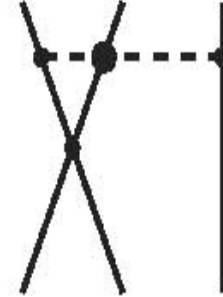
2PE



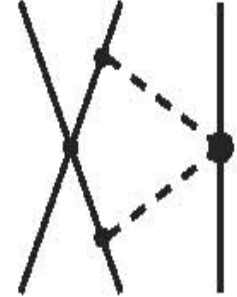
2PE-1PE



Ring



Contact-1PE



Contact-2PE

3NF contacts at N4LO

Girlanda, Kievsky, Viviani, PRC 84, 014001 (2011)

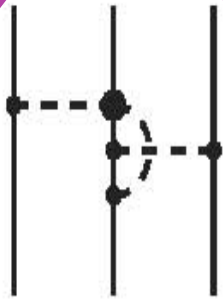
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$$\begin{aligned}
 V = \sum_{i \neq j \neq k} & \left[-E_1 \mathbf{k}_i^2 - E_2 \mathbf{k}_i^2 \boldsymbol{\tau}_i \cdot \boldsymbol{\tau}_j - E_3 \mathbf{k}_i^2 \boldsymbol{\sigma}_i \cdot \boldsymbol{\sigma}_j - E_4 \mathbf{k}_i^2 \boldsymbol{\sigma}_i \cdot \boldsymbol{\sigma}_j \boldsymbol{\tau}_i \cdot \boldsymbol{\tau}_j \right. \\
 & - E_5 (3\mathbf{k}_i \cdot \boldsymbol{\sigma}_i \mathbf{k}_i \cdot \boldsymbol{\sigma}_j - \mathbf{k}_i^2) - E_6 (3\mathbf{k}_i \cdot \boldsymbol{\sigma}_i \mathbf{k}_i \cdot \boldsymbol{\sigma}_j - \mathbf{k}_i^2) \boldsymbol{\tau}_i \cdot \boldsymbol{\tau}_j \\
 & + \frac{i}{2} E_7 \mathbf{k}_i \times (\mathbf{Q}_i - \mathbf{Q}_j) \cdot (\boldsymbol{\sigma}_i + \boldsymbol{\sigma}_j) + \frac{i}{2} E_8 \mathbf{k}_i \times (\mathbf{Q}_i - \mathbf{Q}_j) \cdot (\boldsymbol{\sigma}_i + \boldsymbol{\sigma}_j) \boldsymbol{\tau}_j \cdot \boldsymbol{\tau}_k \\
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 \end{aligned}$$

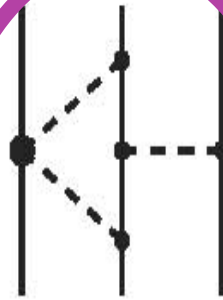
The 3NFs at N4LO

1-loop graphs: 5 topologies

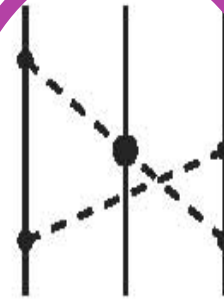
Krebs et al. (2012, 2013)



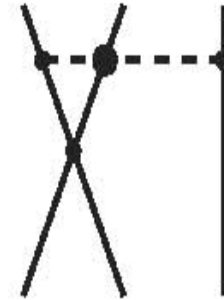
2PE



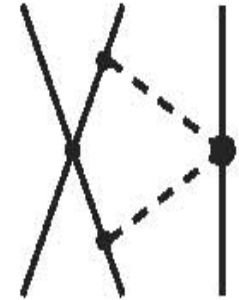
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 & - E_5 (3\mathbf{k}_i \cdot \boldsymbol{\sigma}_i \mathbf{k}_i \cdot \boldsymbol{\sigma}_j - \mathbf{k}_i^2) - E_6 (3\mathbf{k}_i \cdot \boldsymbol{\sigma}_i \mathbf{k}_i \cdot \boldsymbol{\sigma}_j - \mathbf{k}_i^2) \boldsymbol{\tau}_i \cdot \boldsymbol{\tau}_j \\
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 \end{aligned}$$

The 3NFs at N4LO

All possible 20 isospin-spin-momentum/position structures occur!

Krebs, Gasparyan, Epelbaum, PRC 87, 054007 (2013)

Generators \mathcal{G} in momentum space	Generators $\tilde{\mathcal{G}}$ in coordinate space
$\mathcal{G}_1 = 1$	$\tilde{\mathcal{G}}_1 = 1$
$\mathcal{G}_2 = \boldsymbol{\tau}_1 \cdot \boldsymbol{\tau}_3$	$\tilde{\mathcal{G}}_2 = \boldsymbol{\tau}_1 \cdot \boldsymbol{\tau}_3$
$\mathcal{G}_3 = \vec{\sigma}_1 \cdot \vec{\sigma}_3$	$\tilde{\mathcal{G}}_3 = \vec{\sigma}_1 \cdot \vec{\sigma}_3$
$\mathcal{G}_4 = \boldsymbol{\tau}_1 \cdot \boldsymbol{\tau}_3 \vec{\sigma}_1 \cdot \vec{\sigma}_3$	$\tilde{\mathcal{G}}_4 = \boldsymbol{\tau}_1 \cdot \boldsymbol{\tau}_3 \vec{\sigma}_1 \cdot \vec{\sigma}_3$
$\mathcal{G}_5 = \boldsymbol{\tau}_2 \cdot \boldsymbol{\tau}_3 \vec{\sigma}_1 \cdot \vec{\sigma}_2$	$\tilde{\mathcal{G}}_5 = \boldsymbol{\tau}_2 \cdot \boldsymbol{\tau}_3 \vec{\sigma}_1 \cdot \vec{\sigma}_2$
$\mathcal{G}_6 = \boldsymbol{\tau}_1 \cdot (\boldsymbol{\tau}_2 \times \boldsymbol{\tau}_3) \vec{\sigma}_1 \cdot (\vec{\sigma}_2 \times \vec{\sigma}_3)$	$\tilde{\mathcal{G}}_6 = \boldsymbol{\tau}_1 \cdot (\boldsymbol{\tau}_2 \times \boldsymbol{\tau}_3) \vec{\sigma}_1 \cdot (\vec{\sigma}_2 \times \vec{\sigma}_3)$
$\mathcal{G}_7 = \boldsymbol{\tau}_1 \cdot (\boldsymbol{\tau}_2 \times \boldsymbol{\tau}_3) \vec{\sigma}_2 \cdot (\vec{q}_1 \times \vec{q}_3)$	$\tilde{\mathcal{G}}_7 = \boldsymbol{\tau}_1 \cdot (\boldsymbol{\tau}_2 \times \boldsymbol{\tau}_3) \vec{\sigma}_2 \cdot (\hat{r}_{12} \times \hat{r}_{23})$
$\mathcal{G}_8 = \vec{q}_1 \cdot \vec{\sigma}_1 \vec{q}_1 \cdot \vec{\sigma}_3$	$\tilde{\mathcal{G}}_8 = \hat{r}_{23} \cdot \vec{\sigma}_1 \hat{r}_{23} \cdot \vec{\sigma}_3$
$\mathcal{G}_9 = \vec{q}_1 \cdot \vec{\sigma}_3 \vec{q}_3 \cdot \vec{\sigma}_1$	$\tilde{\mathcal{G}}_9 = \hat{r}_{23} \cdot \vec{\sigma}_3 \hat{r}_{12} \cdot \vec{\sigma}_1$
$\mathcal{G}_{10} = \vec{q}_1 \cdot \vec{\sigma}_1 \vec{q}_3 \cdot \vec{\sigma}_3$	$\tilde{\mathcal{G}}_{10} = \hat{r}_{23} \cdot \vec{\sigma}_1 \hat{r}_{12} \cdot \vec{\sigma}_3$
$\mathcal{G}_{11} = \boldsymbol{\tau}_2 \cdot \boldsymbol{\tau}_3 \vec{q}_1 \cdot \vec{\sigma}_1 \vec{q}_1 \cdot \vec{\sigma}_2$	$\tilde{\mathcal{G}}_{11} = \boldsymbol{\tau}_2 \cdot \boldsymbol{\tau}_3 \hat{r}_{23} \cdot \vec{\sigma}_1 \hat{r}_{23} \cdot \vec{\sigma}_2$
$\mathcal{G}_{12} = \boldsymbol{\tau}_2 \cdot \boldsymbol{\tau}_3 \vec{q}_1 \cdot \vec{\sigma}_1 \vec{q}_3 \cdot \vec{\sigma}_2$	$\tilde{\mathcal{G}}_{12} = \boldsymbol{\tau}_2 \cdot \boldsymbol{\tau}_3 \hat{r}_{23} \cdot \vec{\sigma}_1 \hat{r}_{12} \cdot \vec{\sigma}_2$
$\mathcal{G}_{13} = \boldsymbol{\tau}_2 \cdot \boldsymbol{\tau}_3 \vec{q}_3 \cdot \vec{\sigma}_1 \vec{q}_1 \cdot \vec{\sigma}_2$	$\tilde{\mathcal{G}}_{13} = \boldsymbol{\tau}_2 \cdot \boldsymbol{\tau}_3 \hat{r}_{12} \cdot \vec{\sigma}_1 \hat{r}_{23} \cdot \vec{\sigma}_2$
$\mathcal{G}_{14} = \boldsymbol{\tau}_2 \cdot \boldsymbol{\tau}_3 \vec{q}_3 \cdot \vec{\sigma}_1 \vec{q}_3 \cdot \vec{\sigma}_2$	$\tilde{\mathcal{G}}_{14} = \boldsymbol{\tau}_2 \cdot \boldsymbol{\tau}_3 \hat{r}_{12} \cdot \vec{\sigma}_1 \hat{r}_{12} \cdot \vec{\sigma}_2$
$\mathcal{G}_{15} = \boldsymbol{\tau}_1 \cdot \boldsymbol{\tau}_3 \vec{q}_2 \cdot \vec{\sigma}_1 \vec{q}_2 \cdot \vec{\sigma}_3$	$\tilde{\mathcal{G}}_{15} = \boldsymbol{\tau}_1 \cdot \boldsymbol{\tau}_3 \hat{r}_{13} \cdot \vec{\sigma}_1 \hat{r}_{13} \cdot \vec{\sigma}_3$
$\mathcal{G}_{16} = \boldsymbol{\tau}_2 \cdot \boldsymbol{\tau}_3 \vec{q}_3 \cdot \vec{\sigma}_2 \vec{q}_3 \cdot \vec{\sigma}_3$	$\tilde{\mathcal{G}}_{16} = \boldsymbol{\tau}_2 \cdot \boldsymbol{\tau}_3 \hat{r}_{12} \cdot \vec{\sigma}_2 \hat{r}_{12} \cdot \vec{\sigma}_3$
$\mathcal{G}_{17} = \boldsymbol{\tau}_1 \cdot \boldsymbol{\tau}_3 \vec{q}_1 \cdot \vec{\sigma}_1 \vec{q}_3 \cdot \vec{\sigma}_3$	$\tilde{\mathcal{G}}_{17} = \boldsymbol{\tau}_1 \cdot \boldsymbol{\tau}_3 \hat{r}_{23} \cdot \vec{\sigma}_1 \hat{r}_{12} \cdot \vec{\sigma}_3$
$\mathcal{G}_{18} = \boldsymbol{\tau}_1 \cdot (\boldsymbol{\tau}_2 \times \boldsymbol{\tau}_3) \vec{\sigma}_1 \cdot \vec{\sigma}_3 \vec{\sigma}_2 \cdot (\vec{q}_1 \times \vec{q}_3)$	$\tilde{\mathcal{G}}_{18} = \boldsymbol{\tau}_1 \cdot (\boldsymbol{\tau}_2 \times \boldsymbol{\tau}_3) \vec{\sigma}_1 \cdot \vec{\sigma}_3 \vec{\sigma}_2 \cdot (\hat{r}_{12} \times \hat{r}_{23})$
$\mathcal{G}_{19} = \boldsymbol{\tau}_1 \cdot (\boldsymbol{\tau}_2 \times \boldsymbol{\tau}_3) \vec{\sigma}_3 \cdot \vec{q}_1 \vec{q}_1 \cdot (\vec{\sigma}_1 \times \vec{\sigma}_2)$	$\tilde{\mathcal{G}}_{19} = \boldsymbol{\tau}_1 \cdot (\boldsymbol{\tau}_2 \times \boldsymbol{\tau}_3) \vec{\sigma}_3 \cdot \hat{r}_{23} \hat{r}_{23} \cdot (\vec{\sigma}_1 \times \vec{\sigma}_2)$
$\mathcal{G}_{20} = \boldsymbol{\tau}_1 \cdot (\boldsymbol{\tau}_2 \times \boldsymbol{\tau}_3) \vec{\sigma}_1 \cdot \vec{q}_1 \vec{\sigma}_3 \cdot \vec{q}_3 \vec{\sigma}_2 \cdot (\vec{q}_1 \times \vec{q}_3)$	$\tilde{\mathcal{G}}_{20} = \boldsymbol{\tau}_1 \cdot (\boldsymbol{\tau}_2 \times \boldsymbol{\tau}_3) \vec{\sigma}_1 \cdot \hat{r}_{23} \vec{\sigma}_3 \cdot \hat{r}_{12} \vec{\sigma}_2 \cdot (\hat{r}_{12} \times \hat{r}_{23})$

Because of the problems demonstrated, improvement of current nuclear forces indicated

- **How?**
- **Go to next order!**
- **That is: Turn to N4LO.**
- **What can we expect from N4LO?**
- **Does N4LO have anything to offer we were not offered before?**

Oh yes! All 3NFs you have ever dreamed of!



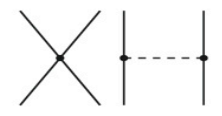
What else is there at N4LO?

2N Force

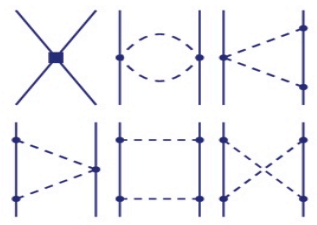
3N Force

4N Force

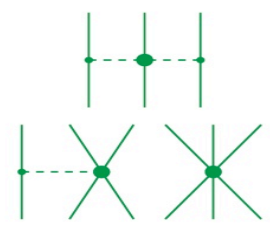
LO
 $(Q/\Lambda_\chi)^0$



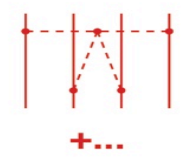
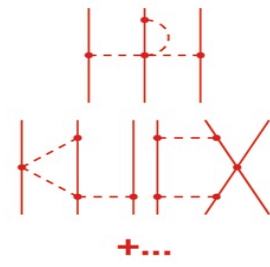
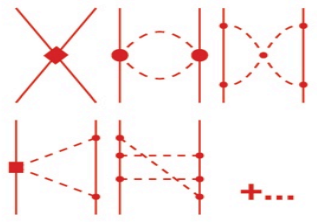
NLO
 $(Q/\Lambda_\chi)^2$



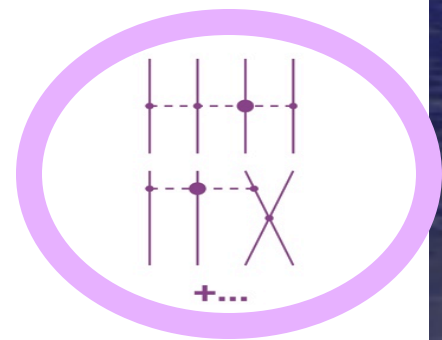
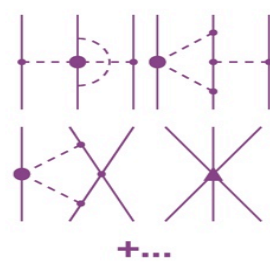
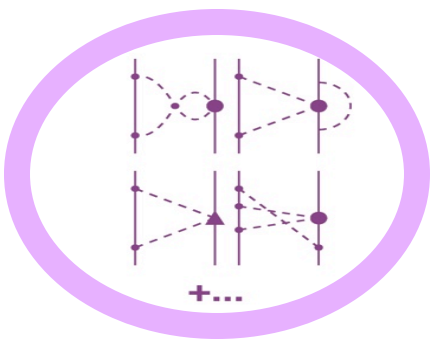
NNLO
 $(Q/\Lambda_\chi)^3$

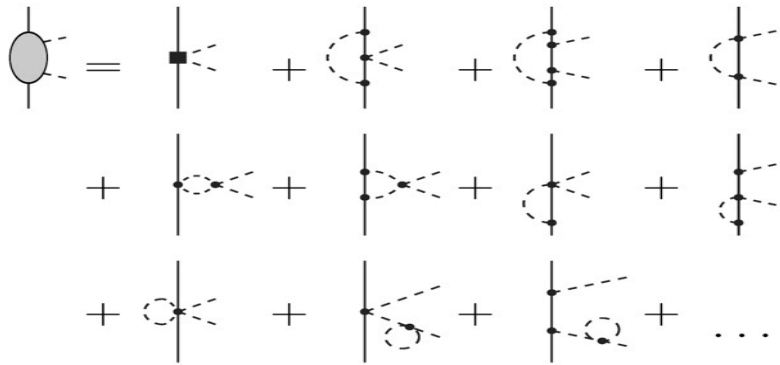
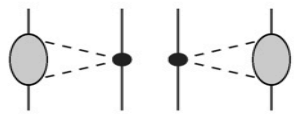


N³LO
 $(Q/\Lambda_\chi)^4$

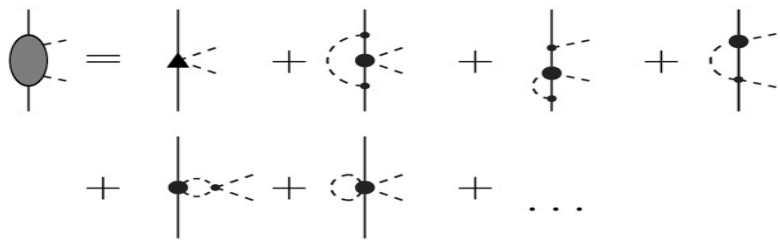
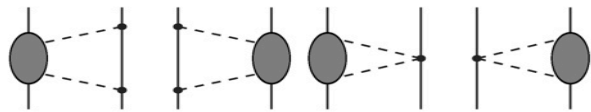


N⁴LO
 $(Q/\Lambda_\chi)^5$

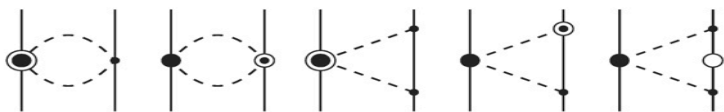




(a)



(b)

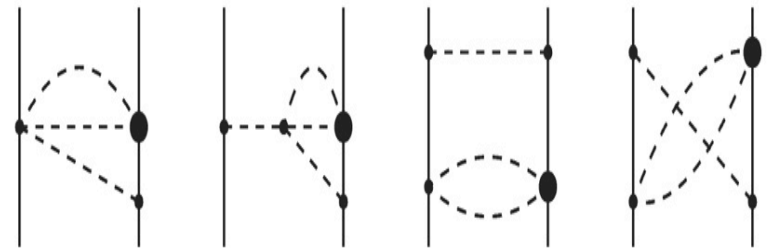


(c)

N4LO 2NF

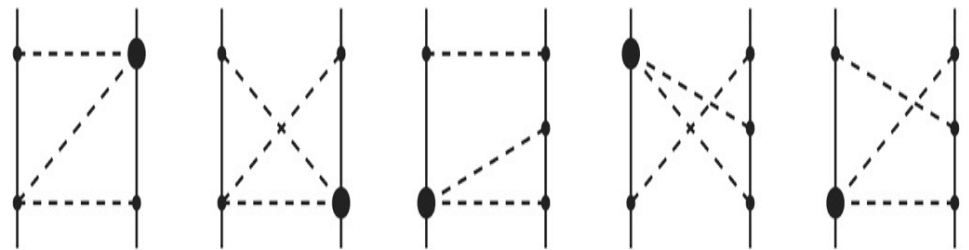
Contributions

Entem, Kaiser, Machleidt, Nosyk,
PRC 91, 014002 (2015)



Class X

Class XI

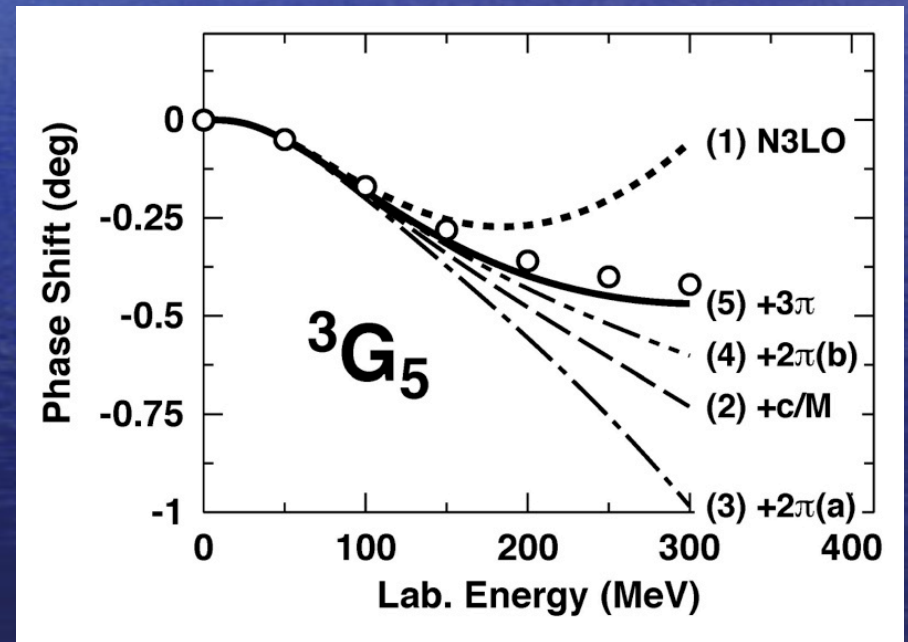
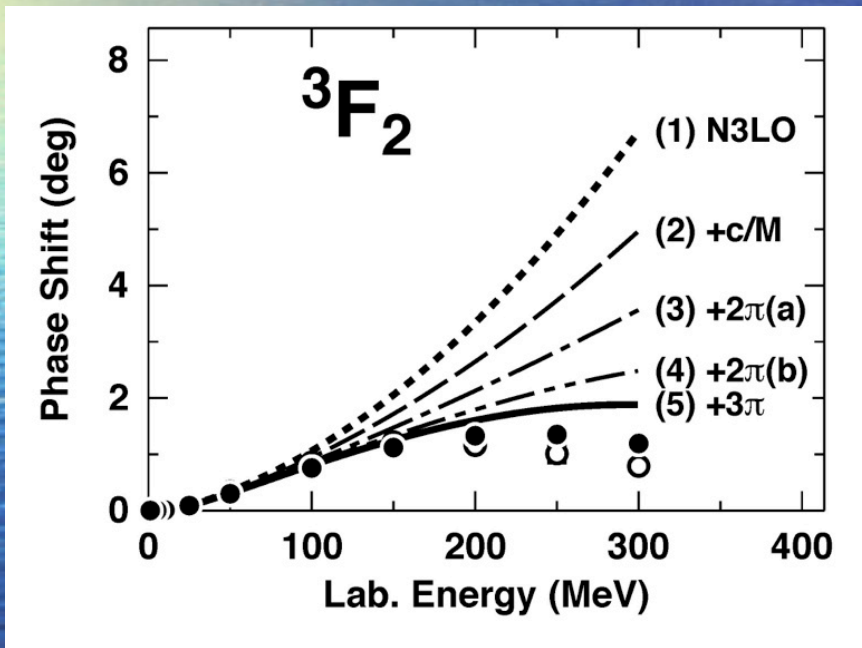


Class XII

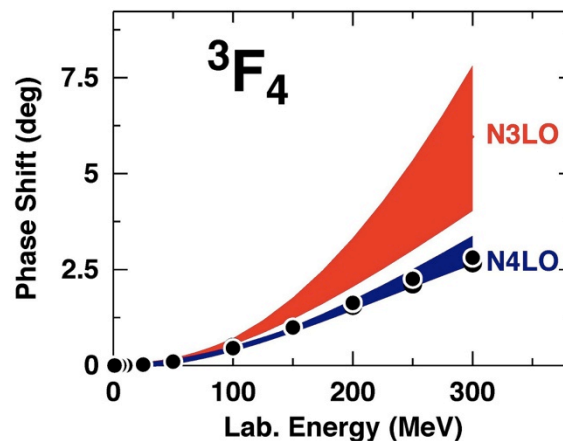
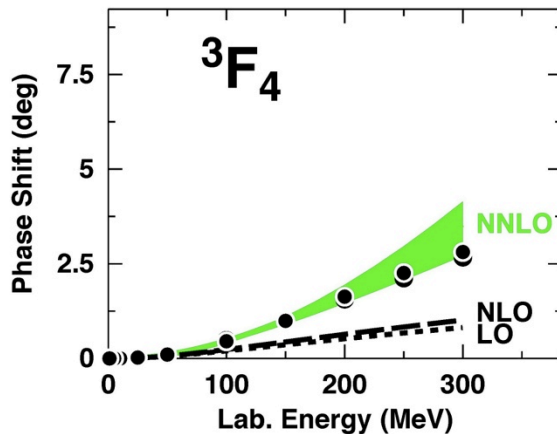
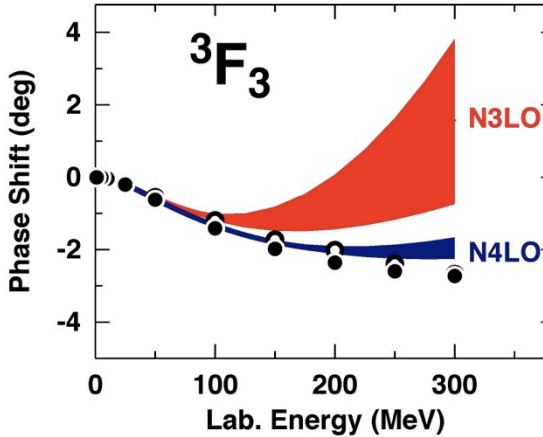
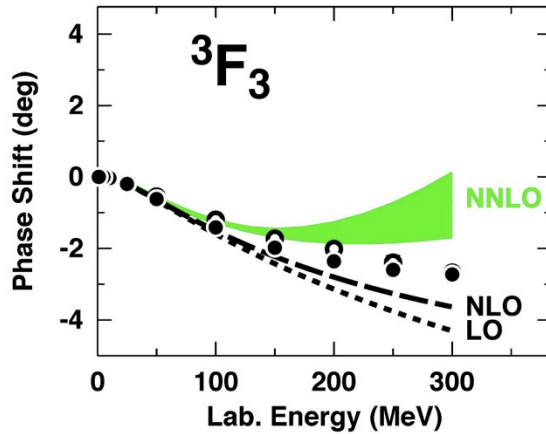
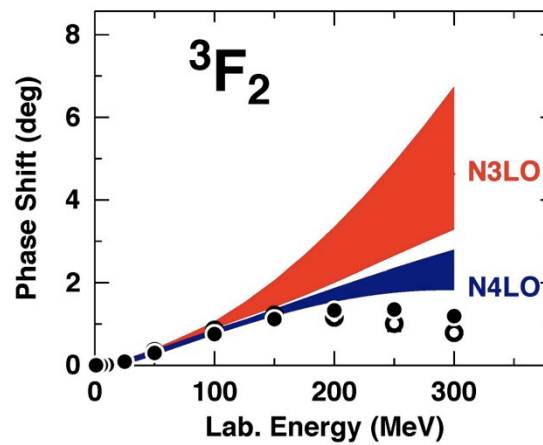
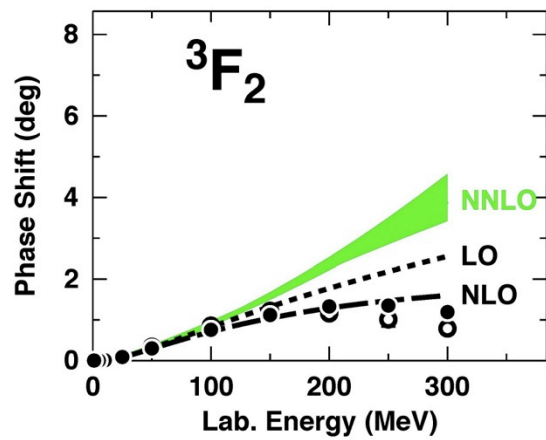
Class XIII

Class XIV

N4LO effects on NN scattering in peripheral partial waves

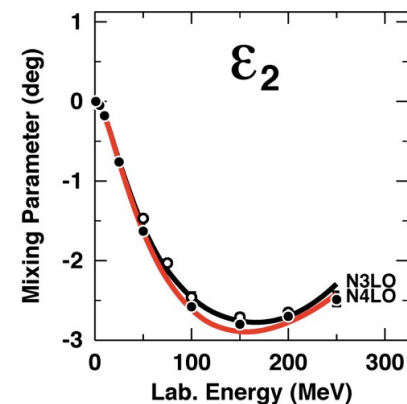
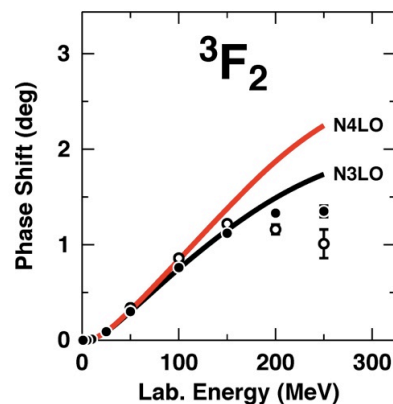
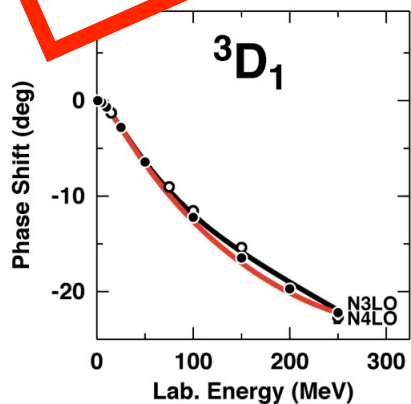
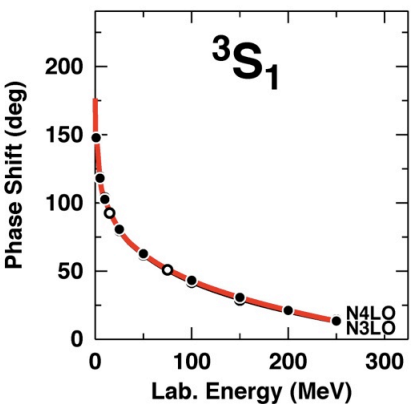
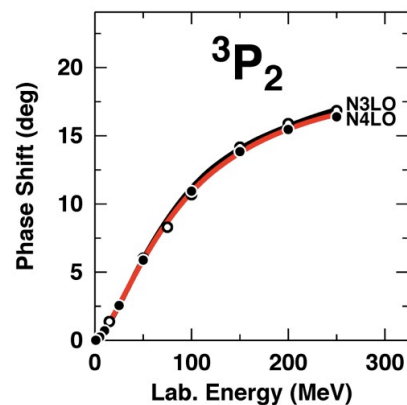
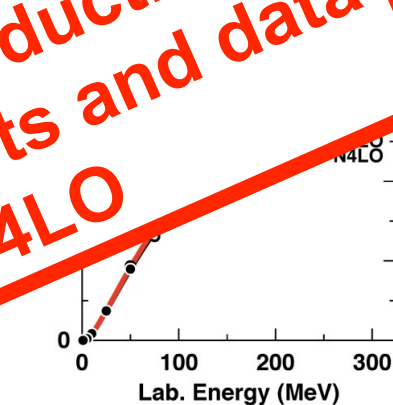
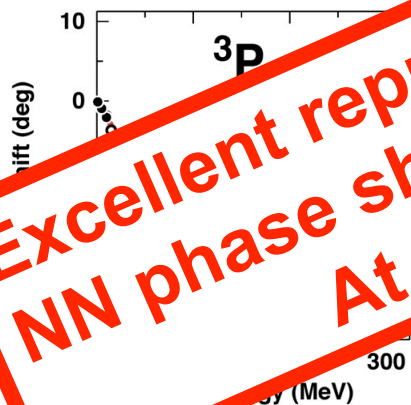
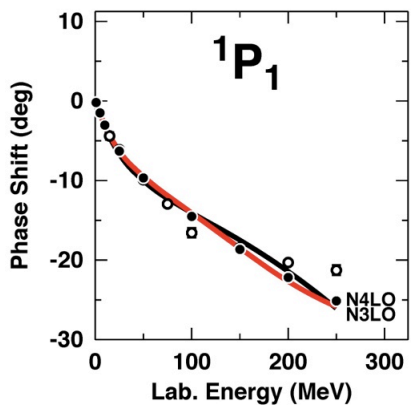
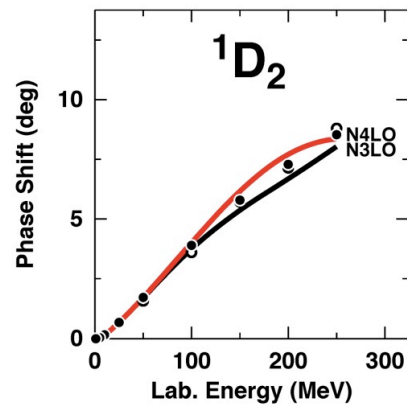
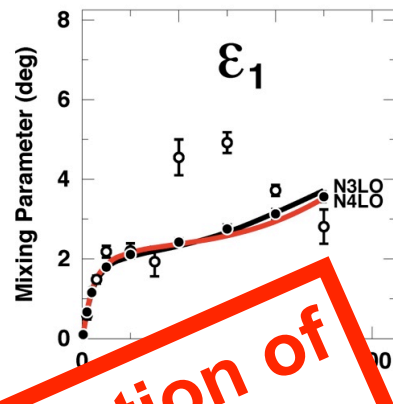
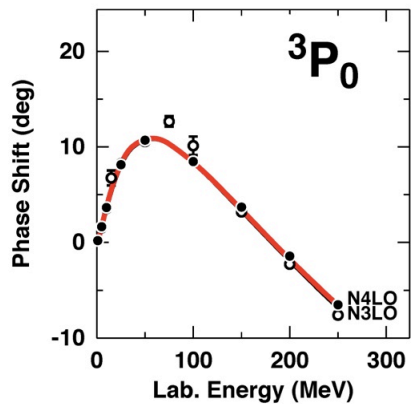
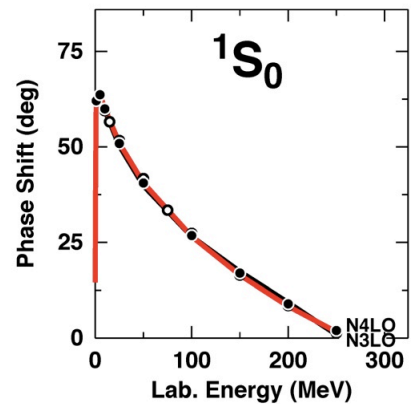


From Entem, Kaiser, Machleidt, Nosyk, PRC 91, 014002 (2015)



Using LECs
from pi-N
Analysis
at order four.

From
Entem, Kaiser,
Machleidt, Nosyk,
PRC 91, 014002
(2015)



Excellent reproduction of NN phase shifts and data At N4LO

Conclusions

- **Be aware of misconceptions!**
- **N3LO won't solve all our problems.**
- **Turn to N4LO: Complete set of 3NFs and new 3NF contacts.**
- **2NF at N4LO promises to be very quantitative including the peripheral waves (N4LO NN pots soon available).**
- **The new challenge and the new hope in microscopic nuclear structure: **N4LO****