Characterizing Early LHC Data in Simple Terms Recent Developments

Natalia Toro Perimeter Institute for Theoretical Physics

Early theory:

Alwall, Arkani-Hamed, Mrenna, Schuster, Thaler, NT, Wang hep-ph/0703088, 0810.3921 Alves, Alwall, Izaguirre, Le, Lisanti, Manhart, Wacker 0803.0019, 1003.3886, 1008.0407 Early Exp:

M. D'Alfonso, J. Incandela, S. Koay, R. Rossin (UCSB) W. Waltenberger (Vienna) C. Horn, A. Schwartzman, et al (SLAC)

Example studies from CERN "Characterization of New Physics II" workshop: <u>http://indico.cern.ch/conferenceOtherViews.py?view=standard&confId=107769</u> SLAC "Topologies for LHC" Workshop: <u>http://www.lhcnewphysics.org/ and http://www-conf.slac.stanford.edu/topologies10/</u>

Characterizing Early LHC Searches

Important questions to ask with the first (null) search results:

- What new-physics possibilities have been excluded?
- Are results from the two experiments compatible?

An excess seen in some **other** search makes both questions more urgent.

- Where else should we look? Are there models that slip through past searches, but could be seen by a different technique?

Progress on each front requires mapping out the boundaries of sensitivity in the broad space of new-physics models, *and beyond the particular model (if any) that motivated the search.*

Inspired by Actual Conversations...

"Hey, I have a great model with 450 GeV gluinos!"

"Are you kidding? LM1 has gluinos at 600 GeV, and is excluded."

"But my model is **nothing** like LM1. For starters, my squarks are heavy so there's no associated production, which is really big for LM1."

- "But your gluinos are so light, they'd still produce tons of them."
- "That's true, but my gluinos decay to several jets. The new search from CMS is best for di-jets. Do you know what its efficiency would be for my gluinos?"

"No. We could ask the people who did the analysis, but they've probably moved on."

What can these two theorists do next?

First Steps

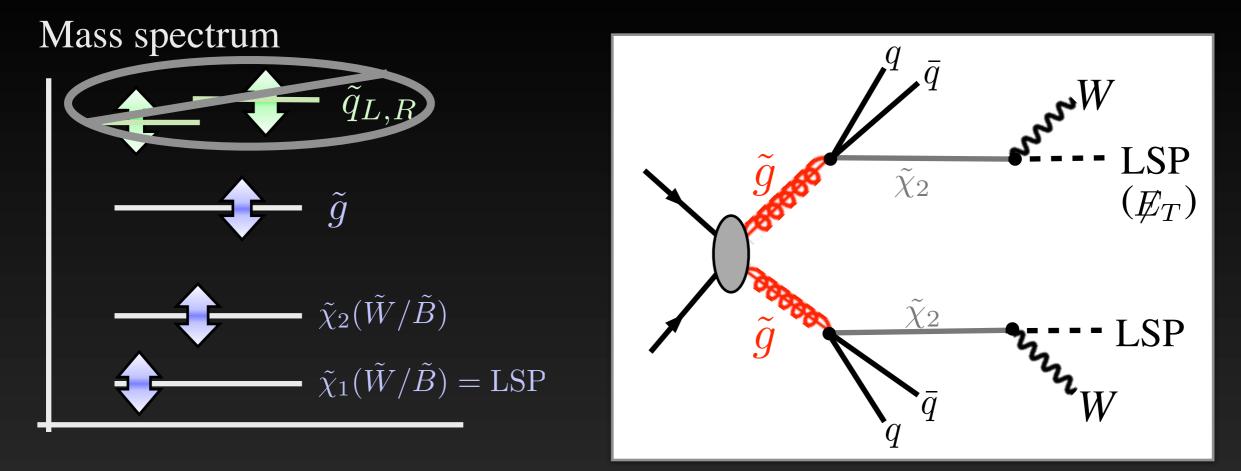
How do we understand search sensitivity to large class of models (even roughly), without expert knowledge of the detector/analysis?

- Estimate sensitivity by running mock-up analysis on signal Monte Carlo (generator-level, PGS, ...), but this is time-consuming, error-prone, not efficiently shared
- Best results can be applied easily & without expert knowledge

Partial, short-term solution: identify & study re-usable building blocks.

- *Partial:* Fully complete list is impossible
- Short-term: When one (or a few) tractable models are clearly preferred by data, use it to get precision results!
 ...I expect this will take a while.

Processes: Re-Usable Building Blocks

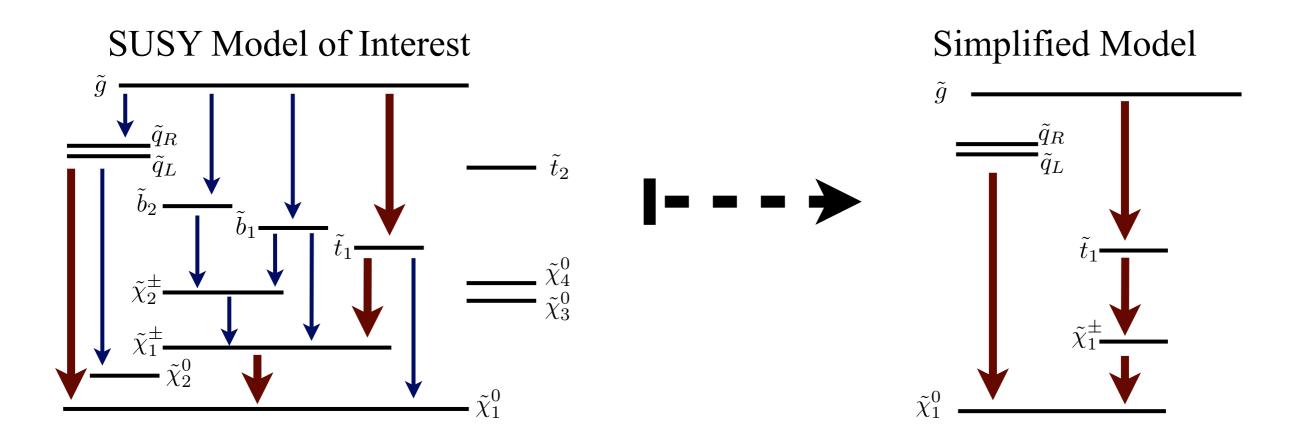


Masses of $\tilde{g}, \tilde{\chi}_2, \tilde{\chi}_1$ affect kinematics, search efficiency/optimization

Cross-section depends on unknowns (spins & masses of other particles), but scale is known (QCD gluino production)

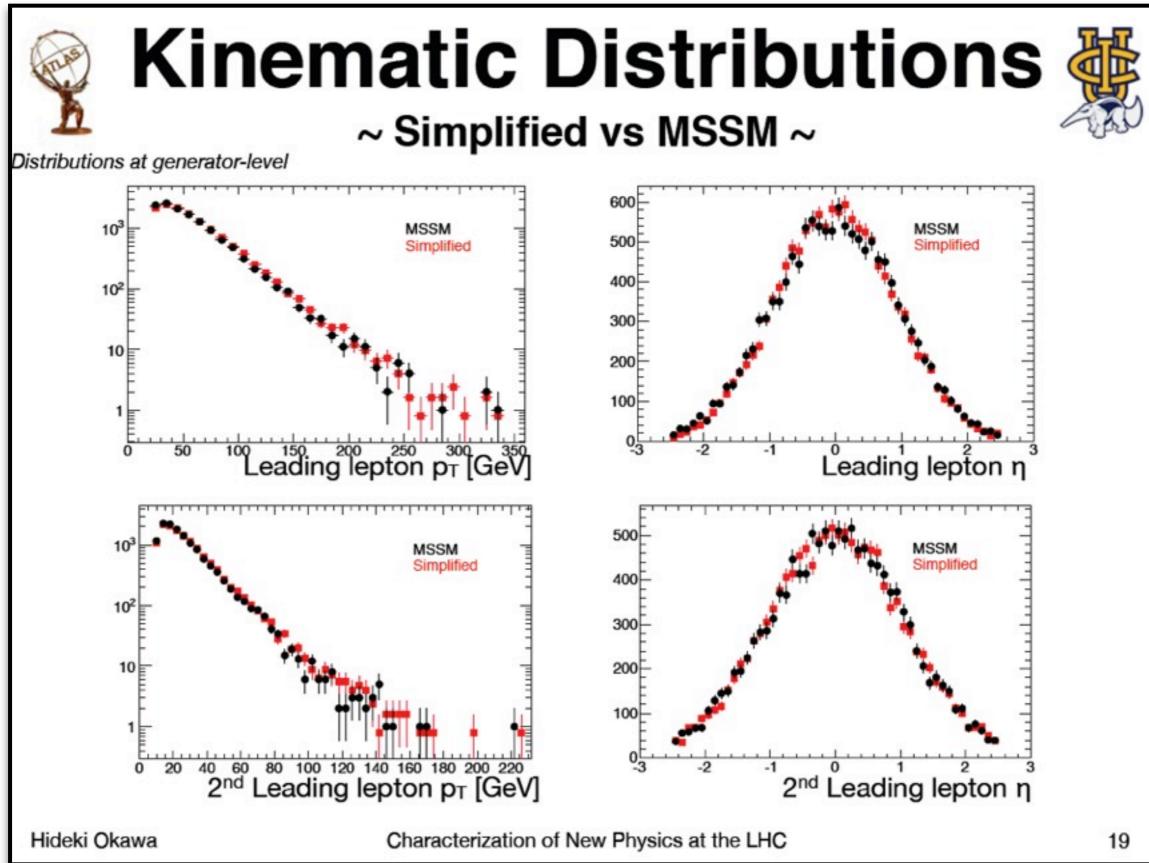
These parameters are simply related to observables, **and** simple to calculate in given model.

Simplified Models <u>Example</u>



Most **Simplified Models** are perfectly valid models (this one is a limit of the MSSM), **built to emphasize features that matter in a collider search**

Slide from Hideki Okawa's talk: <u>http://indico.cern.ch/getFile.py/access?</u> <u>contribId=22&resId=0&materialId=slides&confId=107769</u>



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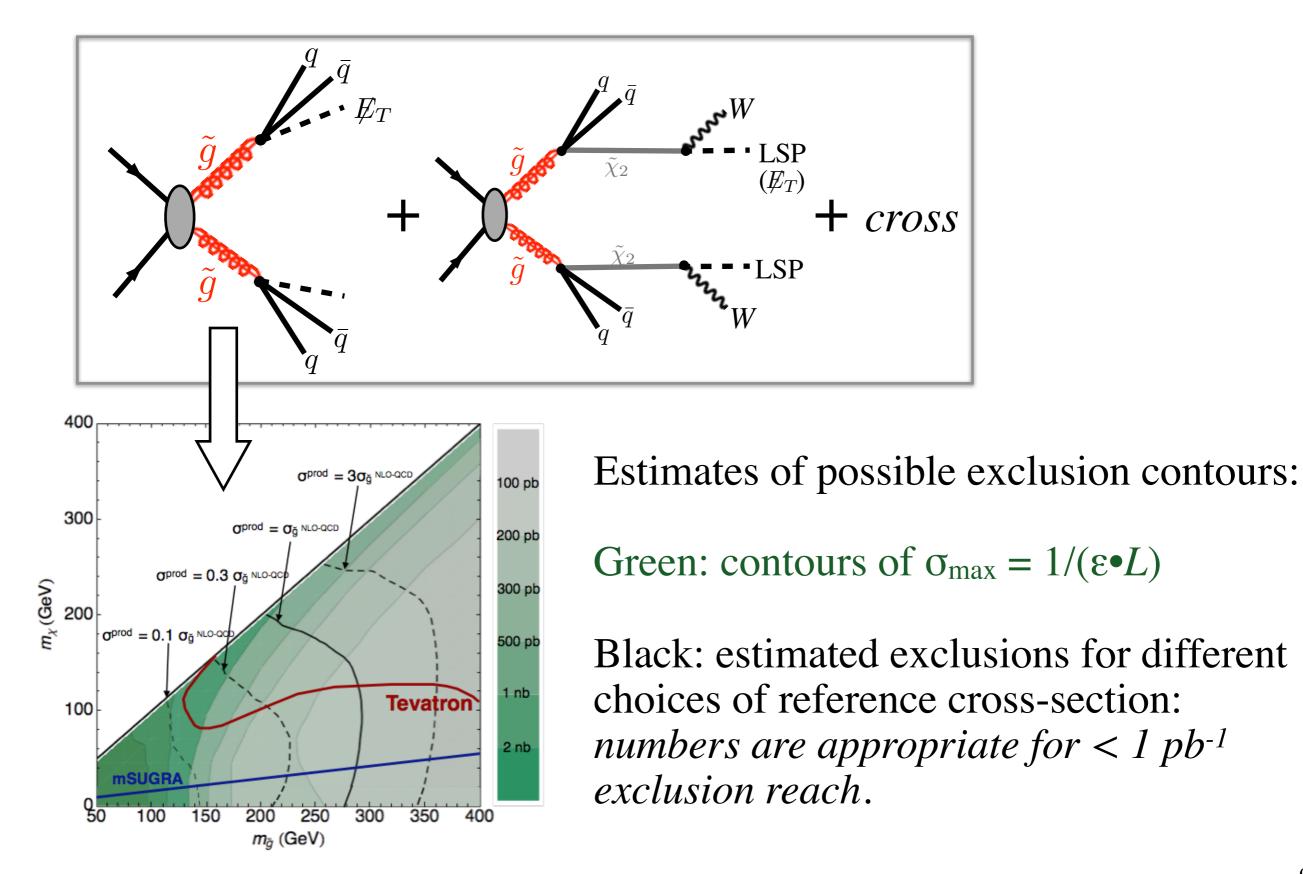
Outline

- 1. Example: Simplified Model Limits
 - What do they look like?
 - How are they used?

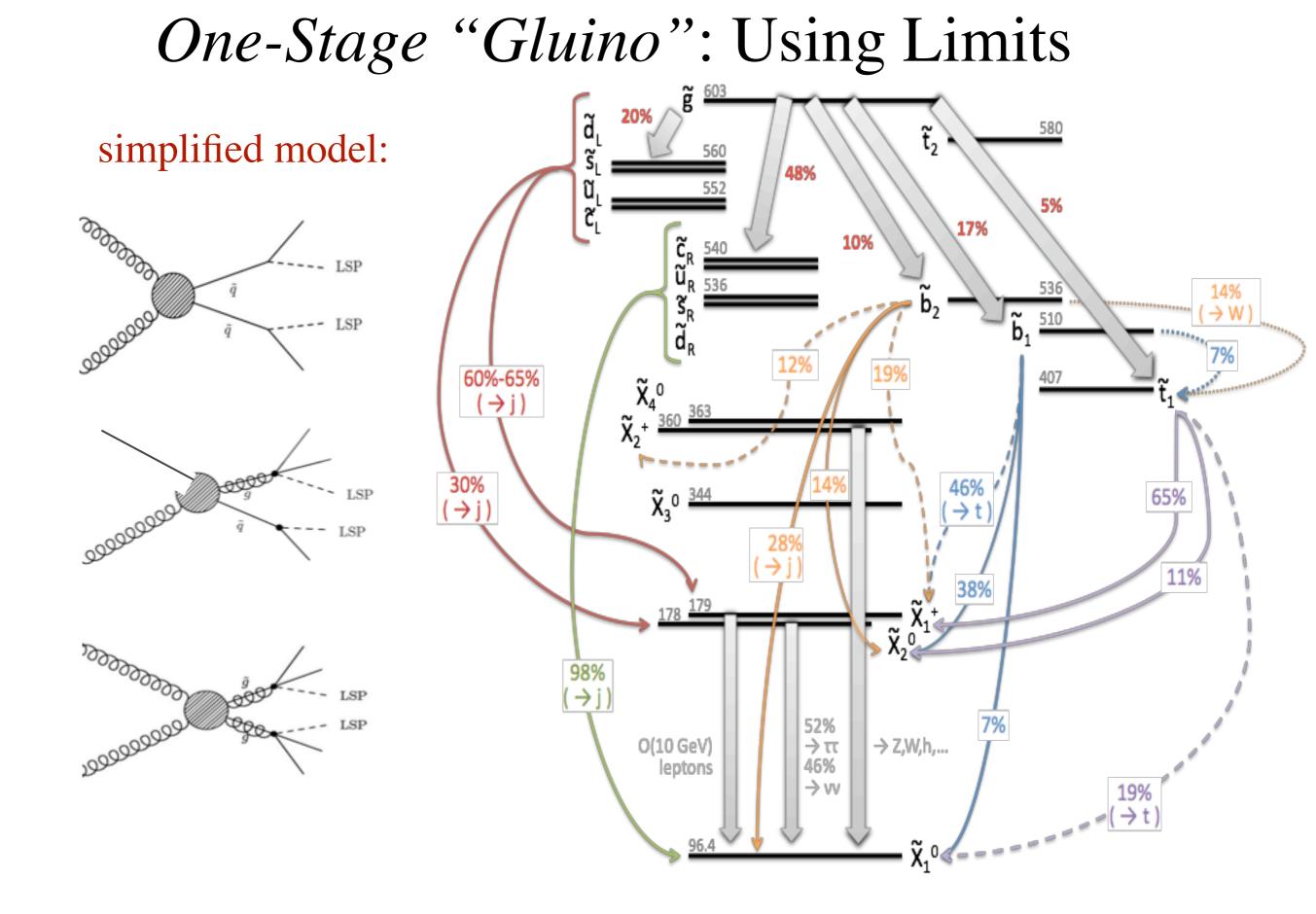
"What can we put in papers besides mSUGRA plots and raw distributions, to make them more useful?

- 2. Identifying and Using Simplified Models (SUSY Example)
 - What makes a good simplified model?
 - Simplified Models for 50 pb⁻¹ SUSY Searches
- 3. A growing database of simplified models
 - SLAC Topologies Workshop (Enumeration)
 - <u>http://lhcnewphysics.org</u> (Implementation & Reference)

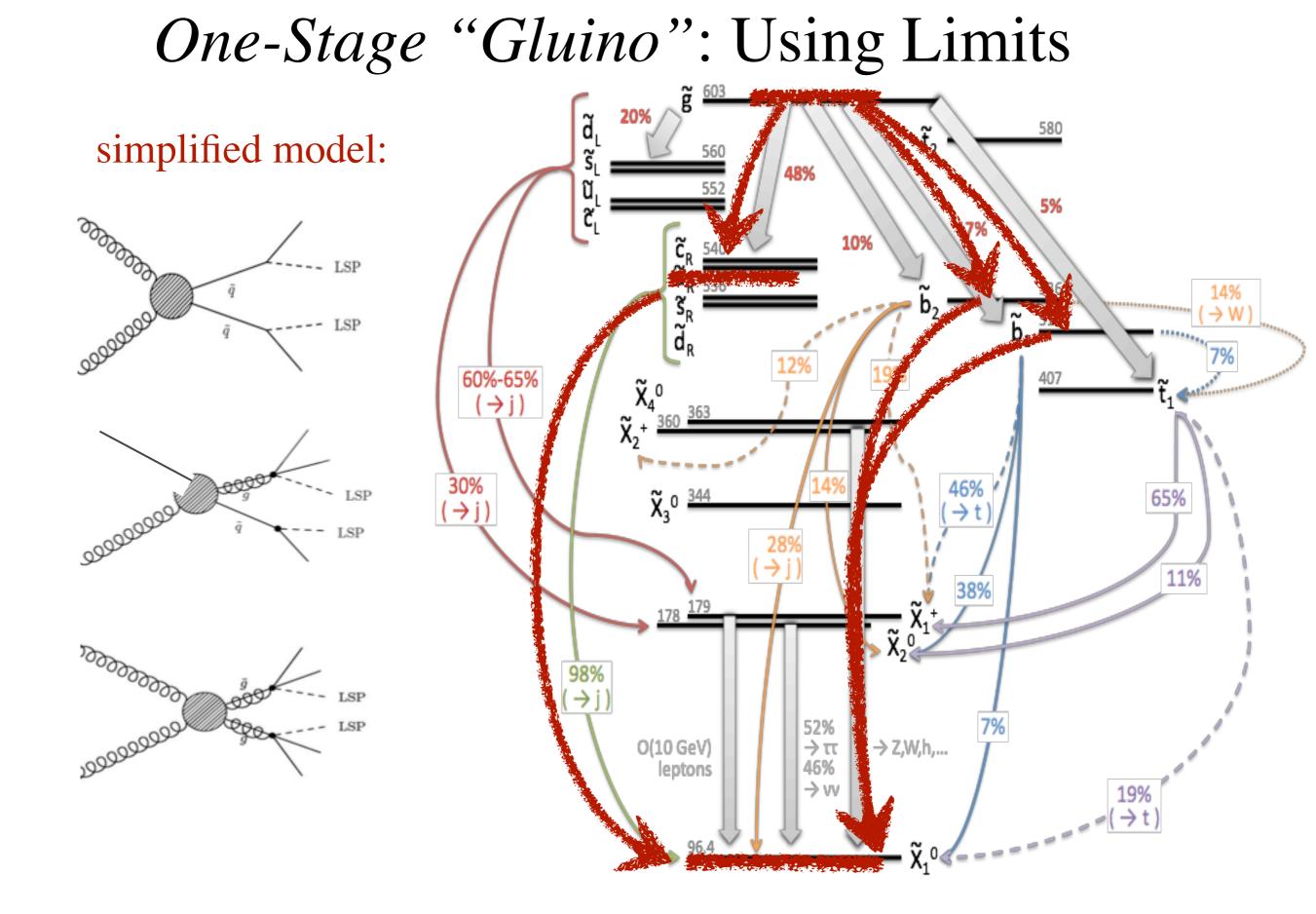
One-Stage "Gluino": Quoting Limits



[Plots from Alvez, Izaguirre, Wacker; see also lhcnewphysics.org "Gluino One-Stage"]

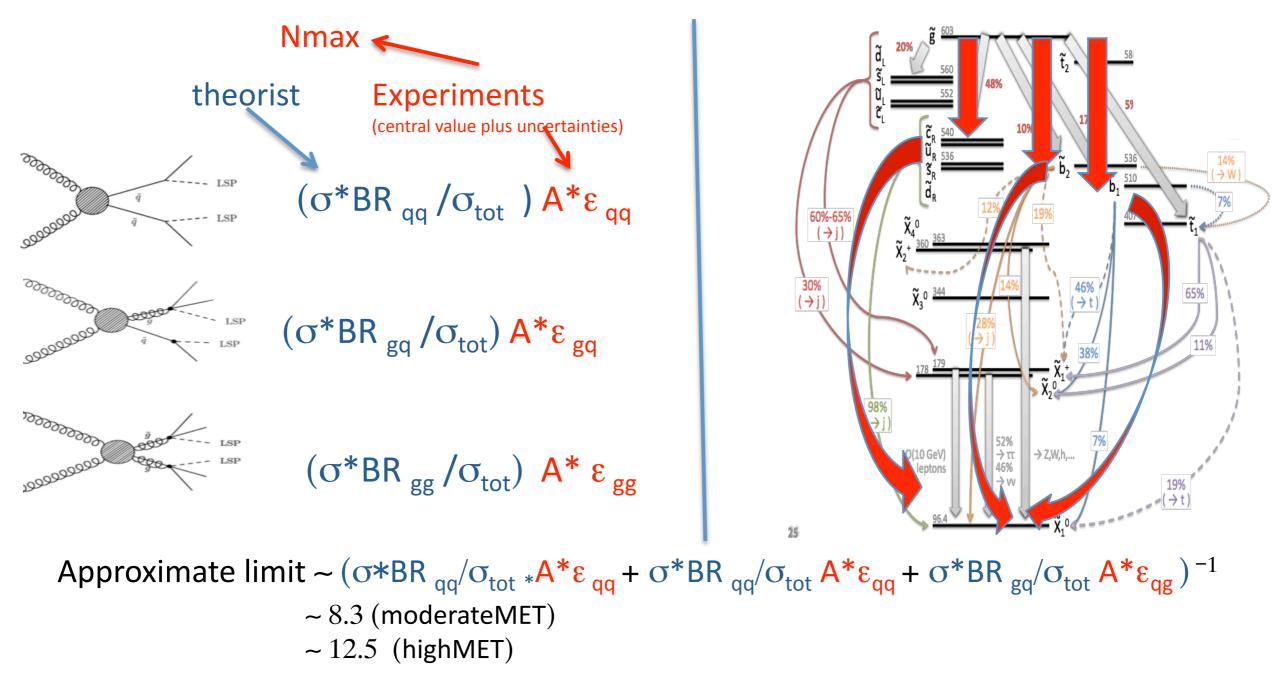


Is this model excluded? Depends on (cross-section) x (acceptance) 10



Is this model excluded? Depends on (cross-section) x (acceptance) 10

Approximate approach



Full blown LM1 limit ~ $1/(\sigma^*BR^*\epsilon) \sim 6.6$ (moderateMET) ~ 10 (highMET)

(use less info. \rightarrow weaker limit by ~25%)

[M. D'Alfonso, CNP2 CERN] 11

Summary

- This is **one** of the ways that topology-level results are extremely useful to the rest of the world.
 - Complementary to what theorists already do external mockups of analysis

here, experimental details are all handled by experimental experts

- Complementary to what experimentalists already do parametrizing search impact in individual models less optimal limit, but vastly broader
- Valuable no matter how search is optimized/motivated but offers natural language for theory-experiment collaboration on extending searches.
- Very useful way to build/convey intuition about search sensitivity.

- Why is simplified model limit only 20% worse, with limited information?
 - LM1 is easy case "mostly" direct decays to LSP (80% of \tilde{g} decays, 98% of \tilde{q}_R decays
 - Search is more efficient for these decays than for cascades leaving out ~40% of generated events cost only 25% in σ·acceptance
- Is search sensitive to models that go **dominantly** through cascade decays? Do these allow lighter superpartners?
 - Not addressed by LM search, or simplified model search unless it's extended to include more topologies

In particular, valuable to include **two-cascade** decay modes to study this case!

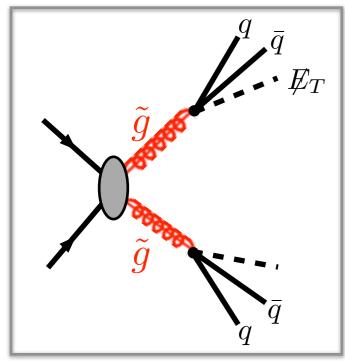
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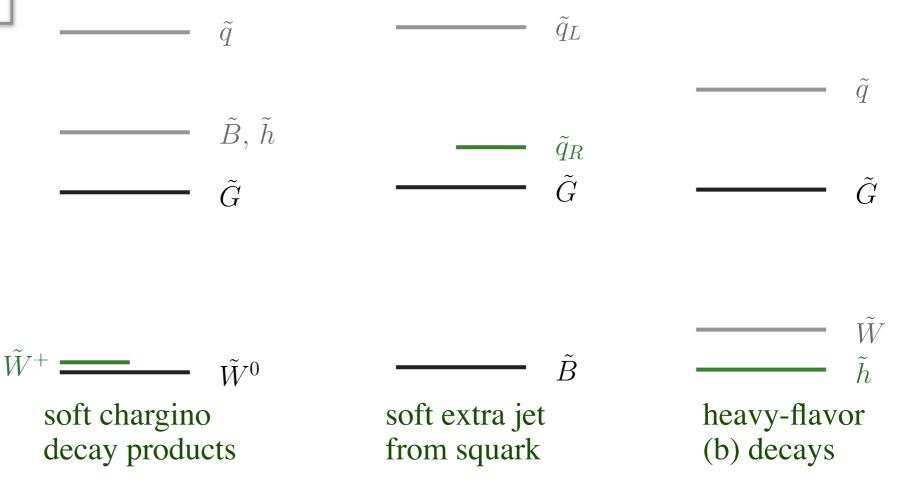
Hadronic SUSY



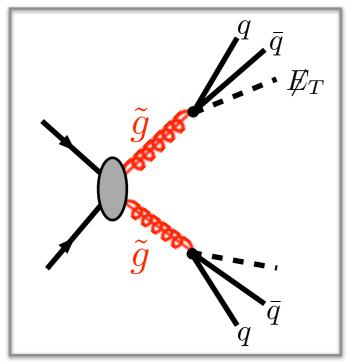
Ubiquitous production/decay mode for SUSY with neutralino LSP

For some MSSM spectra, this mode dominates

For others, it is a **good proxy for dominant modes**



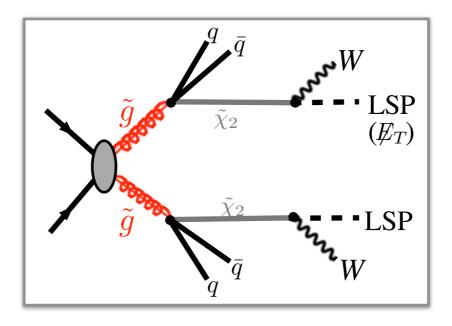
Hadronic SUSY



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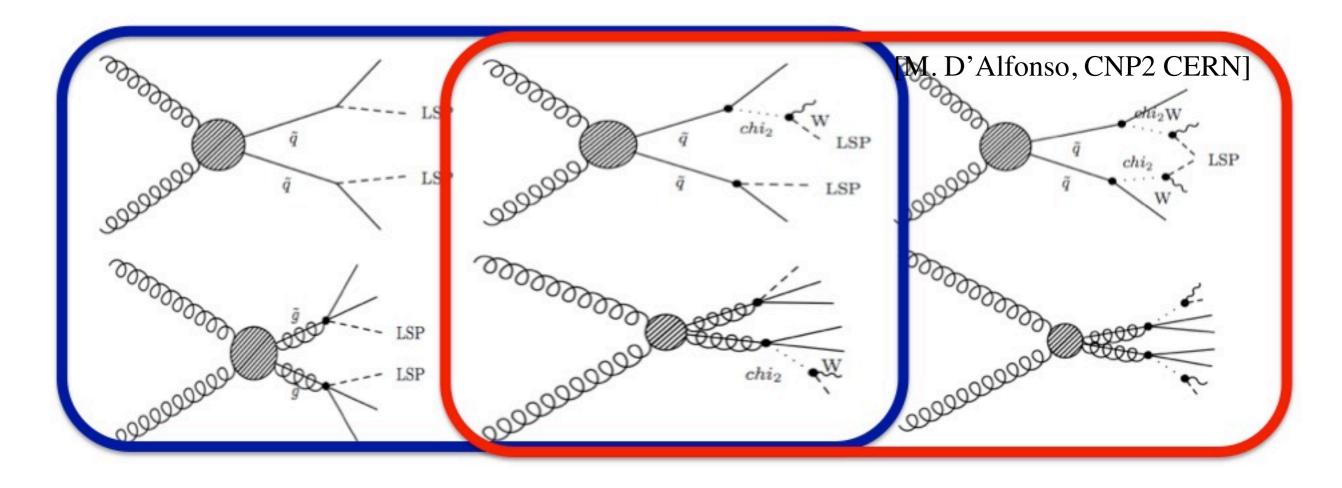
For others, it is a good proxy for dominant modes

For other spectra, **very different modes dominate** – cascade decays



– squark production– decays through top

Simplified Model for SUSY with 0/1 leptons

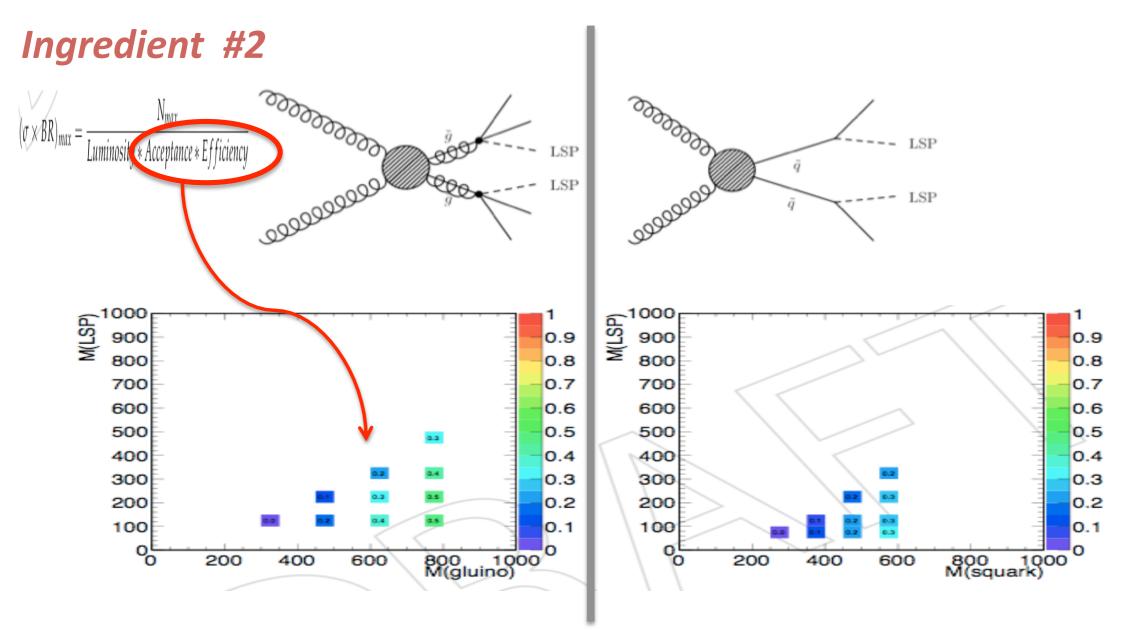


For hadronic search, consider hadronic W/Z in cascades For 1-lepton search, consider leptonic W.

Parameters to scan for each topology: Gluino, LSP, χ_2

Acceptance*efficiency

Hadronic analysis



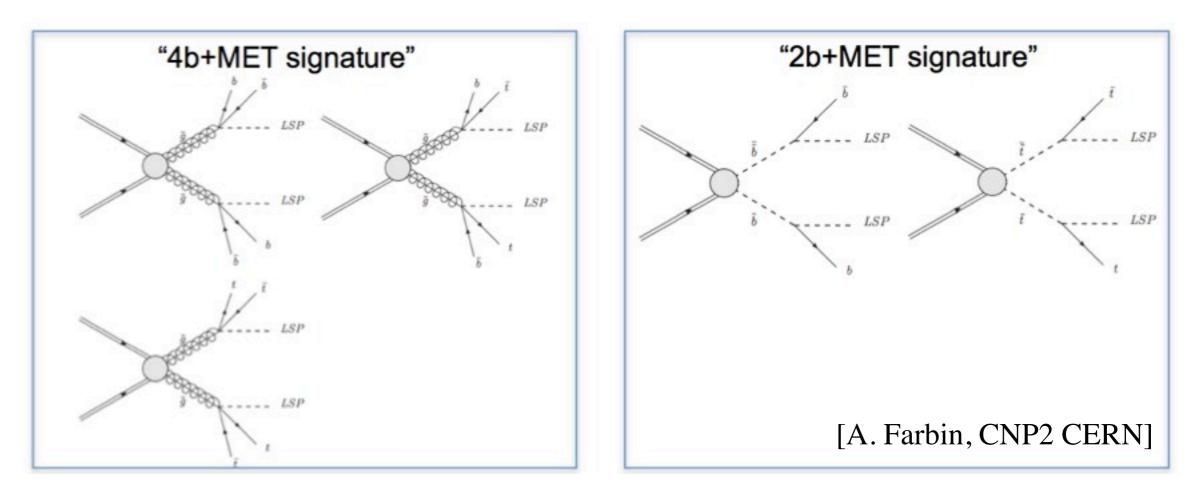
Comments #2:

Do we need to split the acceptance*efficiency into two pieces ? If yes, we need to define what constitutes "acceptance" and "efficiency"

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[M. D'Alfonso (UCSB CMS), CNP2 CERN]

Heavy-Flavor Models

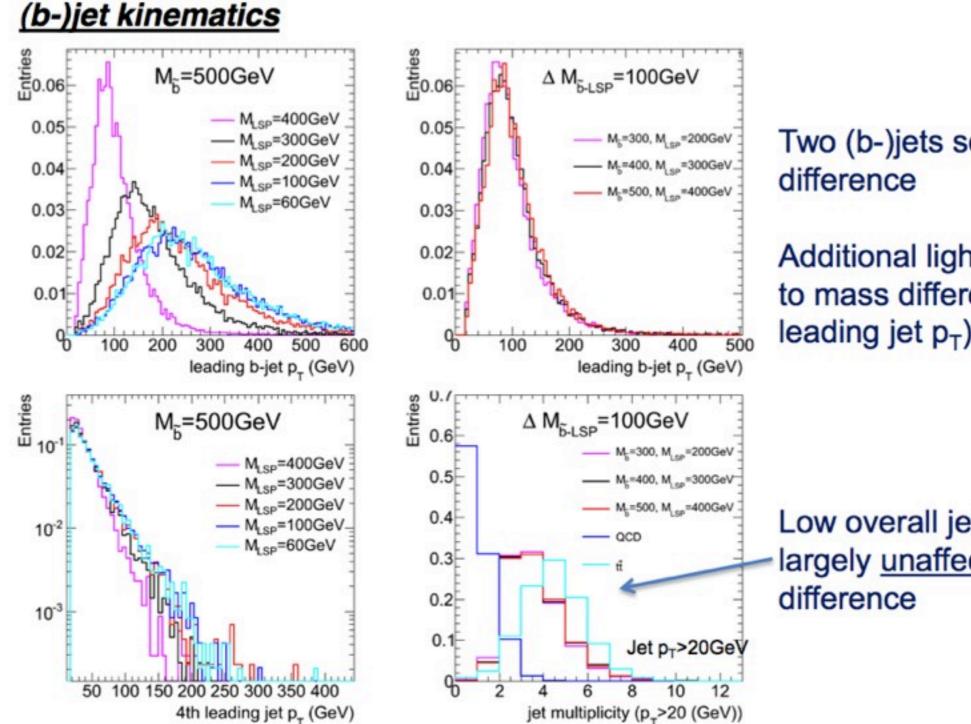


t-rich gluino decays \Rightarrow different jet kinematic distributions *b*-rich gluino decays \Rightarrow alternate handle on SM backgrounds

Beautiful *b*-tagging in early LHC: opportunity to do this search soon!

High theoretical impact — b/t-rich decays dominate in direct mediation models (heavy u/d/s/c squarks), models w/ less fine-tuned m_Z ! ¹⁹

Squark production: 2b+MET



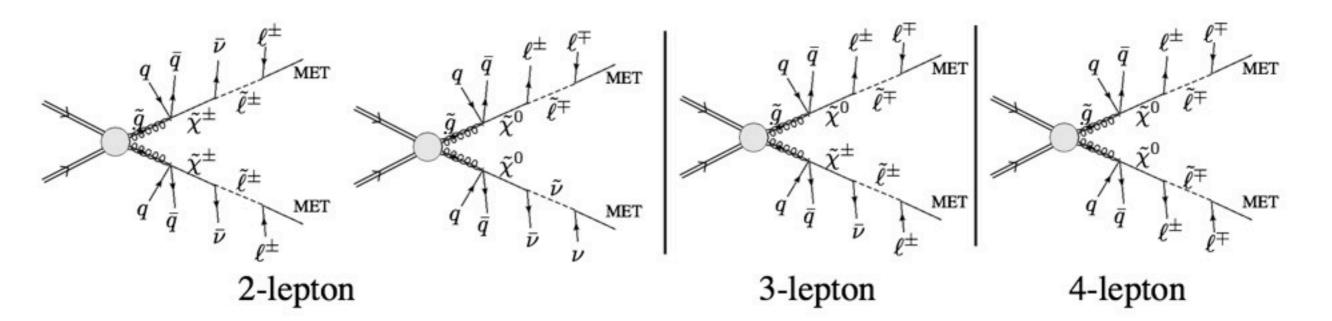
Two (b-)jets sensitive to mass

Additional light jets not sensitive to mass difference (see 4th leading jet p_T)

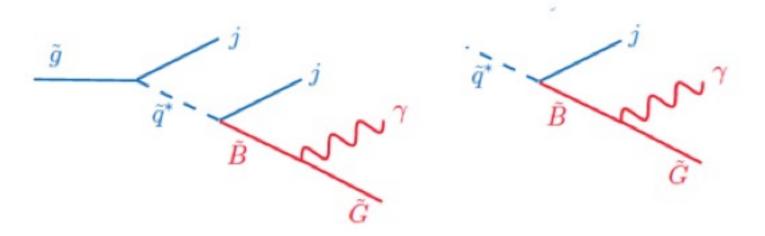
Low overall jet multiplicity: largely unaffected by mass

[P. de Jong (ATLAS) SLAC Topo Wkshop] 20

Multi-Leptons, Photons



Motivated by GMSB ($m_{MET} = 0$ gravitino) and models with $m_{3/2} \sim \text{TeV}$ ($m_{MET} \ge 50$ GeV neutralino)



Searches are typically much less sensitive to kinematics and jettiness of initial production!

New Physics vs. Simplified Models

Enough about exclusions!

How do simplified models help us if there **is** new physics?

Caveats:

optimistic treatment – background subtracted w/o systematic errors to illustrate qualitative points.

"true new physics" in this example was deliberately chosen to be complicated and **unlike** our simplified models

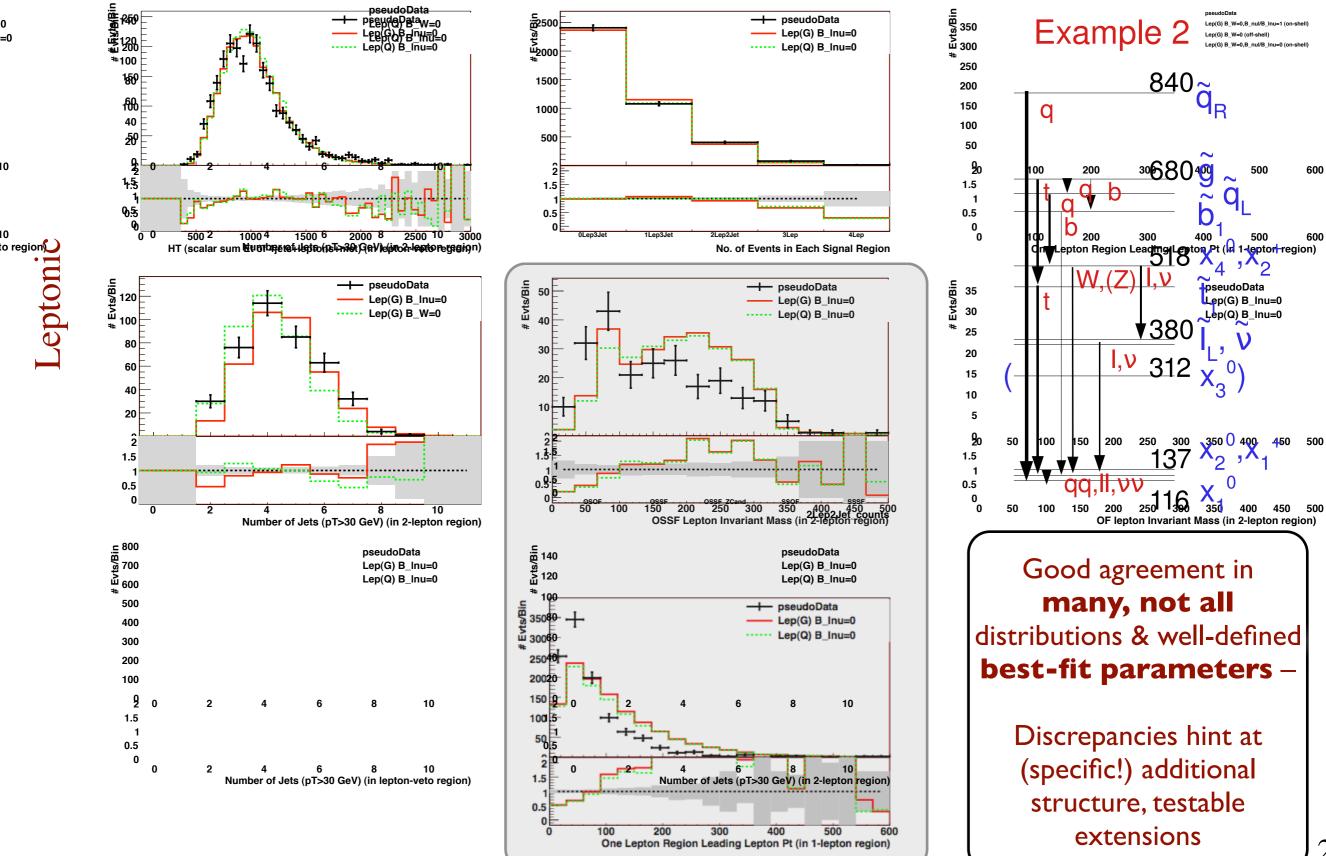
[uses simplified models from 0810.3921]

New Physics vs. Simplified Models

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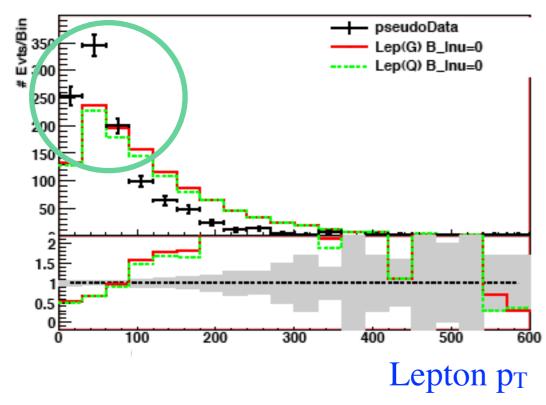
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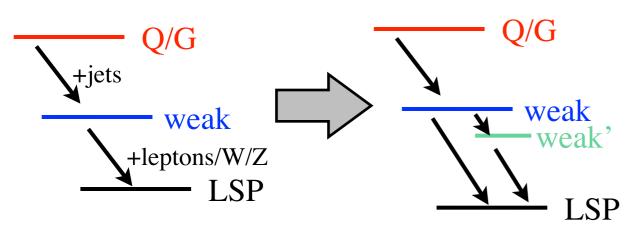


Inferring structure from simple characterization

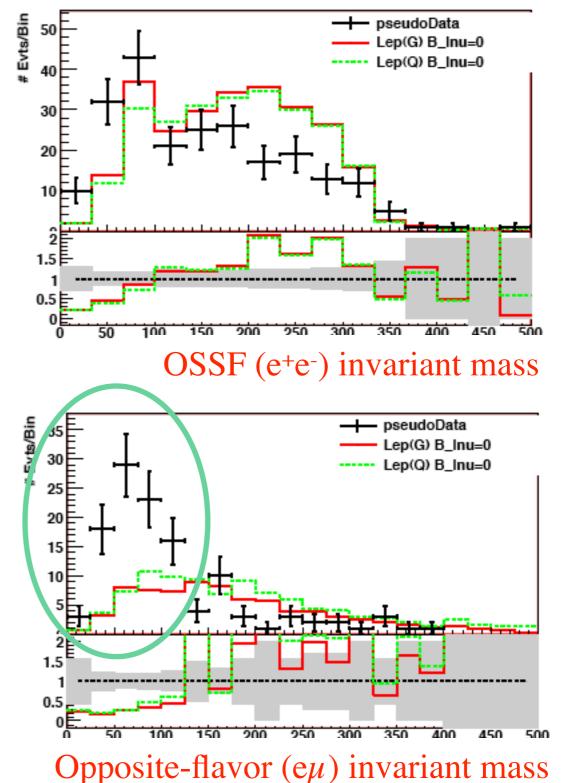
(1-lepton plots)



STRONG EVIDENCE for more complex source of soft, flavor-uncorrelated leptons.



(2-lepton plots)



Add and subtract intermediate particles to "prove" their existence!

Workshop on Topologies for Early LHC Searches

http://www.lhcnewphysics.org/

<u>http://www-conf.slac.stanford.edu/topologies10/</u> Organizers: R. Essig, M. Lisanti, P. Schuster, T. Tait, N. Toro, J. Wacker

Over 100 theorists (mostly model builders) proposed a baseline set of simplified models for early LHC searches.

Working groups (subset of active contributors):

Leptons	Hadrons	Resonances	Exotic Objects	Heavy Flavor
S. Chang	D. Alves	Y. Bai	S. Chang	M. Buckley
W. Cho	J. Gainer	H. Cheng	M. Baumgart	R.S. Chivukula
J. Evans	M. Gomez	J. Evans	R. Essig	L. Fitzpatrick
E. Izaguirre	E. Izaguirre	A. Freitas	J. Hubisz	R. Francescini
J. Kaplan	C. Kilic	T. Han	D. Krohn	P. Fox
M. Lisanti	M. Nojiri	J. Hewett	P. Meade	J. Kaplan
M. Luty	D. Krohn	T. Liu	D. Morrissey	P. Ko
M. Nojiri	M. Schwartz	V. Rentala	M. Papucci	E. Kuflik
T. Okui	J. Shelton	S. Su	D. Phalen	R. Lu
M. Park	M. Spannowsky	T. Tait	J. Shao	S. Mrenna
M. Perelstein	M.Strassler		T. Volansky	M. Peskin
J. Ruderman	J. Wacker		I. Yavin	K. Rehermann
V. Sanz		Photons	K. Zurek	M. Schmaltz
P. Schuster				M. Schwartz
D. Shih		P. Fox		E. Simmons
S. Su		R. Kitano		C. Spethmann
T. Tait		T. Okui		M. Strassler
B. Thomas		D. Shih		T. Tait
N. Toro		T. Roy		N. Toro
J. Wacker		J. Ruderman		W. Waltenberger
F. Yu				5

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Hadronic (Flavor-Blind) Simplified Models

	With MET		No MET		
# jets	2→1	2→2	2→1	2→2	2→3
1	Composite gluon: $pp \rightarrow g^* \rightarrow g \phi(invis)$ KK gluon (2- or 3-body): $pp \rightarrow g_2 \rightarrow \gamma_1 g_1 \rightarrow g \gamma_1 \gamma_1$ $pp \rightarrow g_2 \rightarrow j \gamma_1 \gamma_1$	ISR+invis. Z' ISR+invis. pair Squark+neutralino	_		
2	Resonance	KK quark or squark pair	dijet resonances	Compositeness, anomalous running of α_s	Anomalous $(G_{\mu\nu})^3$
3	A→B¢ B→ jets	Squark/			
≥4	$\phi \rightarrow invis.$	gluino pair	Resonant coloron	Techni-π, RPV squark/ gluino	

Heavy-Flavor-Rich (t/b/ τ) Simplified Models

	Source of b/τ's		
	Resonance	Pair	Cascade
Has flavor	Vector-like heavy	Stop/sbottom	stau NLSP
quantum no.	quark	$t' \rightarrow b/t + g/\gamma/W/Z$	3rd-gen-rich RPV
Unflavored	Z', W' with	Gluino→heavy flavor	h→ φ φ → 4b/τ
	enhanced 3rd	Color-adjoint scalar	h→ bb in SUSY
	gen. couplings	Higgs cascades	decay

Topologies '10 Progress

<u>http://www.lhcnewphysics.org/</u> (improved searchable site in progress)

Exotics WG

- High Multiplicity (M. Baumgart, J. Hubisz, K. Zurek)
- Displaced Vertices, models 1 and 2 (S. Chang, D. Morrissey)
- Weird Jets (D. Krohn, M. Papucci, D. Phalen)
- = dE/dx, Timing, and Weird Tracks (R. Essig, P. Meade, J. Shao, T. Volansky, I. Yavin)

Resonances WG

- S-channel gamma gamma Resonance (Joanne Hewett, Tao Liu, Viram Rentala)
- Tau-tau resonances (Ayres Freitas, S Jets WG
- Excited Quark decaying to jZ or j gam
- Fourth Generation Leptons decaying
- Leptoguarks (Hsin-Chia Cheng, Yang
- Authors: D. Alves, C. Kilic Doubly Charged Higgs" decaying to
- Technimeson decaying into 3 EW bos
- R-parity violating-like decays into goc
- Diboson Resonances(gamma gamma) Bai, Jared Evans, Ayres Freitas)

Photon WG

- Dark Matter + ISR photon (P. Fox)
- Vectorlike Confinement: Weak (T. Ok)
- Vectorlike Confinement: Strong (T. Ol
- Excited Quark (R. Kitano, T. Roy)
- General Neutralino NLSP (Yuri Gerst) Thomas, Yue Zhao)

Lepton WG

[edit]

- Models like SUSY with Bino LSP (Mariangela Lisanti, Veronica Sanz) H⁺⁺⁺ models, W'/Z' models (Shufang Su) Maximal flavor-violating scalar (Felix Yu) Same-Sign Trileptons (Takemichi Okui, Brooks Thomas) Chargino decays via staus (Won Sang Cho) Models like susy w/sneutrino lsp (Won Sang Cho, Mihoko Nojiri, Myeonghun Park, Maxim Pereistein) 2 Same-Sign Dileptons in Supersymmetry and Extra-Dimensions (Veronica Sanz) One-Stage Gluino Cascade Decays (Philip Schuster, Natalia Toro, Jay Wacker, Eder Izaguirre) 4+ Jet Final States Without MET Multi-Lepton GMSB (Richard Gray, Michael Park, Josh Ruderman, David Shih, Sunil Somalwar, Scott Thomas, Yue Zhao) Heavy Flavor (Bottom/Top/Tau) WG [edit] Multi-Leptons from Direct Electroweak Mariangela Lisanti, Jared Kaplan) Non-Resonant Production [edit] Technicolor-Inspired Simplified Model I Authors: M. Buckley, R. Franceschini, P. Fox, J. Kaplan, E. Kuflik, R. Lu, S. Mrenna, M. Peskin, Production (Spencer Chang, Jared Eva 5/7j & no MET (pp->go squark->5/7j) M. Strassler, N. Toro Multijet using 2ⁿ model (M. Strassler) Pair production to four heavy flavors (without MET) 2-3 Jet Final States Without MET Heavy flavor production from Higgs Decays Higgs to 4 taus Stop and/or Sbottom-Like Topologies G^3 coupling (pp->3) (no missing) Bluon partners production with t/b decays and W/Z single-stage cascades 2j & no MET (4 fermion, 2 quark 2 gluon or 4 gluon operators) Vectorlike Top Quark changed QCD beta function (maybe with Jay and Matt Strassler) and Generation Leptoquarks and Diquarks (Ben Gripaios) a 3j & no MET (not clear there exists interesting new models) Taus from SUSY with light gravitino, stau NLSP (To Be Added) and Generation from R-Parity Violation Heavy Flavor Production From Gluino Pair Production (Rouven Essig, Jared Kaplan) Resonant-Production [edit] Authors: R.S. Chivukula, L. Fitzpatrick, P. Ko, K. Rehermann, M. Schmaltz, M. Schwartz, E. Simmons, C. Spethmann, T. Tait, W. Waltenberger Neutral singly-produced resonances decaying to heavy flavor Charged singly-produced resonances decaying to heavy flavor Right-handed W' in 4-body heavy flavor final state Single production of vectorial heavy guark
- = 2->2: 2j+MET (M. Gomez, E. Izaguirre) = 2->2: 3j+MET (M. Gomez, E. Izaguirre)

Multi-Jets + MET

4j & no MET (pp->XX->4j)

4 & no MET (pp->Y->XX->4)

6j & no MET (pp->go go->6j)

Authors: J. Gainer, M. Schwartz

- = 2->2: 4j+MET (M. Gomez, E. Izaguirre)
- Multi-Jet+MET from an initial resonance (J. Shelton and M. Spannowsky)
- = 2->2 (2j + MET) for simplified Little Higgs / UED like model. Spin correlation. (M. Nojiri)

Single-Jet + MET Simplified Models

Authors: M. Strassler, J. Wacker

- Squark-Neutralino associated production
- Composite gluon to invisible + jet
- 2nd KK gluon to KK squarks -> quark LSP
- Invisible Z' with ISR
- Additional Contributors: D. Krohn

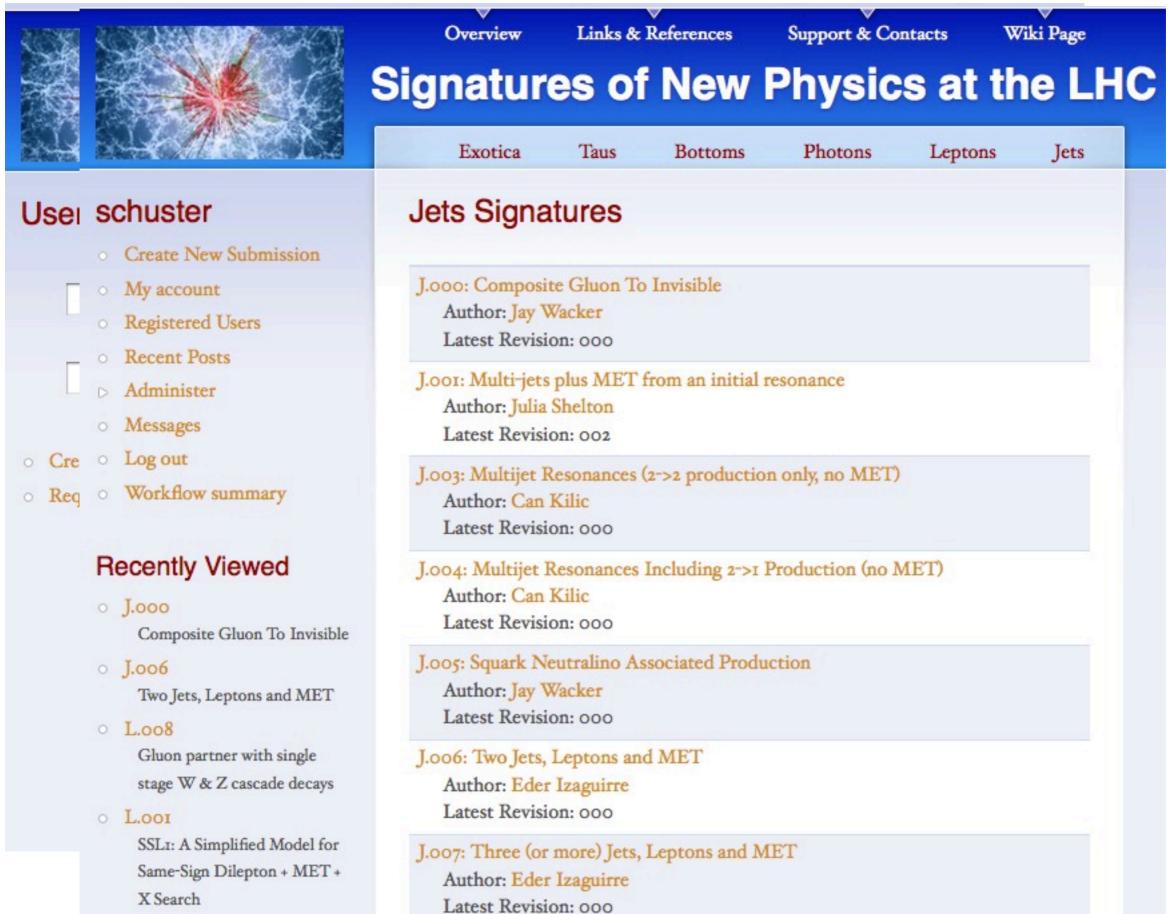
Writeups for simplified models including:

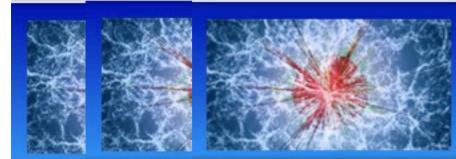
- Particle content & interactions
- Theoretical motivation
- MC generation tools & support
- Estimated past limits (when possible)
- Relevant variables/plots
 - -Kinematic vars of interest
 - -Parameter space for limits
- Estimated LHC reach, and possible challenges

important for optimizing searches. Particular attention was paid to including

topologies inspired from a broad array of well-motivated theories.







Use schust schuster



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Recently Recently Viewed

o B.000 o J.000 Heavy Flavor Gluino Decays Compo o L.000 o J.006 4 leptons +MET or 6-lepton Two Je final states from R-parity L.008 violation Gluon L.008 stage V Gluon partner with single 0 L.001 stage W & Z cascade decays SSLI: A 0 1.006 Same-S Two Jets, Leptons and MET X Searc o J.000

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Photons

Bottoms

Leptons

Jets

Heavy	Flavor	Gluino	Decays
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Submission Information

Abstract:

Exotica

We define a collection of topologies motivated by the production of states with an affinity for the 3rd generation. Specifically, we consider production of color octet gluon-partner particles that decay to pairs of top or bottom quarks, or a top-bottom pair, along with missing energy from a new particle (such as a stable neutralino in supersymmetry). We also include the possibility of extra on or off-shell W and Z bosons from cascades as a possible add-on. LaTex Source File:

Tex file

Submission PDF Version:

d GluinoHeavyFlavor.pdf

Approved:

no

Add new comment

HeavyFlavor leptons MET SSDL SUSY

Comments



SSLI: A

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Two Jets, Leptons and MET

Cor

A Module for Heavy Flavor Topologies

New Physics Working Group, www.lhcnewphysics.org Contact Authors: Rouven Essig and Jared Kaplan Email contact: questions@lhcnewphysics.org

I. INTRODUCTION

In this note, we define a collection of topologies motivated by the production of states with an affinity for the 3rd generation. Specifically, we consider production of color octet gluon-partner particles that decay to pairs of top or bottom quarks, or a top-bottom pair, along with missing energy from a new particle (such as a stable neutralino in supersymmetry). We also include the possibility of extra on or off-shell W and Z bosons from cascades as a possible add-on. Gluon partners are very well-motivated by considerations of naturalness, and supersymmetry provides an example of a concrete model (we assume that these new particles carry a parity, so that they are always pair produced and their decays are accompanied by missing energy). We collect topologies indicative of gluon partner production with decays into heavy flavors into topology modules with precise rules for Monte Carlo simulation.

First, we will define a module with direct decays to $t\bar{t} + E_T$ and $b\bar{b} + E_T$ to capture the most generic topologies. Since the particle that carries away missing energy may naturally have a nearly degenerate charged SU(2) partner, we add a cascade resulting in $tbW^{(*)} + E_T$, where the W^{\pm} may be far off-shell so that it is basically invisible. We also provide 'add-on' modules with cascade decays that involve W^{\pm} and Z^0 bosons. Future extensions to this framework might include more complicated cascade decays.

II. DEFINITION

The basic module we are proposing is the following:

 G is the gluon partner. The spin can be 0, ¹/₂, or 1. The mass parameter is M_G, and is a free parameter.

Conclusion

- Search results can be made much more practically usable for studying TeV-scale physics, with (small) additional characterization.
- Simplified models organize production/decay topologies to
 - Allow almost-back-of-the-envelope study of search sensitivity to models
 - Easily parametrize 'gaps' in a search, where different approach is called for
- A broad list of simplified models inspired by **many** models and signatures is available.
 - Experimentalists: please use this resource in presenting results!
 - Th & Exp: Feel free to add/comment on the website <u>http://www.lhcnewphysics.org</u>

BACKUP

Simplified Model MC

- Pythia or MadGraph: take "simple spectrum" limit of an implemented model, e.g. SUSY, by decoupling unnecessary states be careful, input masses aren't always physical masses!
 - RMSS(1)=100 ! bino RMSS(2)=1205 ! decouple wino
 RMSS(3)=600 ! gluino RMSS(6)=1000 ! decouple slepton-L
 RMSS(8)=550 ! left-squark RMSS(9)=1500 ! decouple squark-R
 ...etc...
- Pythia: SLHA or native decay tables for 'invented' simplified model particles (can be automated using Marmoset)

DECAY 6000004 1.00	# gluino	
0.50000	$2 -6000003 \qquad \# \rightarrow q \qquad \sim qba$	r
0.50000	$-2 6000003 \# \rightarrow \text{qbar} \sim \text{q}$	
DECAY 6000003 1.00	# squark	
1.00000	$2 1000022 \# \rightarrow q LSP$	

• MadGraph/FeynRules: User models (assumed spin-dependent couplings of new-physics particles dictate matrix elements)

Differences:

LSP

- Treatment of initial-state radiation, decay matrix elements (can be important on tails, small elsewhere)
- Easy implementation of general models vs. generality

Limit Interpretation

- Highest-precision exclusion on a model is always dedicated analysis but too many models of interest
- Approximate exclusions readily obtained from topology limits

$$(\sigma \times \varepsilon)_{\text{model}} = \sum_{XY \to \mathcal{A}} (\sigma_{XY} \times \mathcal{B}_{\mathcal{A}}) \times (\varepsilon_{XY \to \mathcal{A}})$$
 Detector
response to process process

For each search:

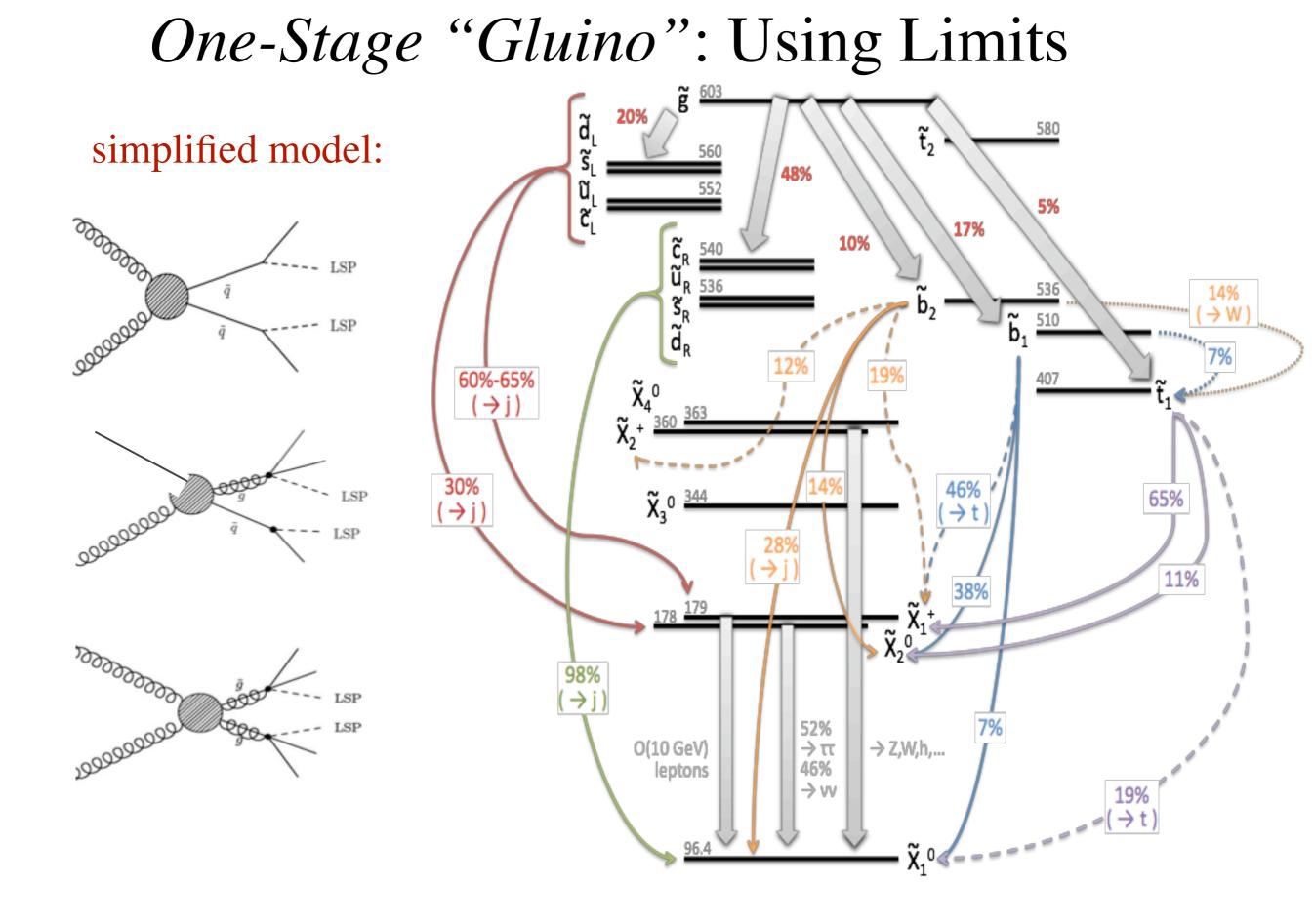
1) Simplified-model limits encode statistics & process efficiency

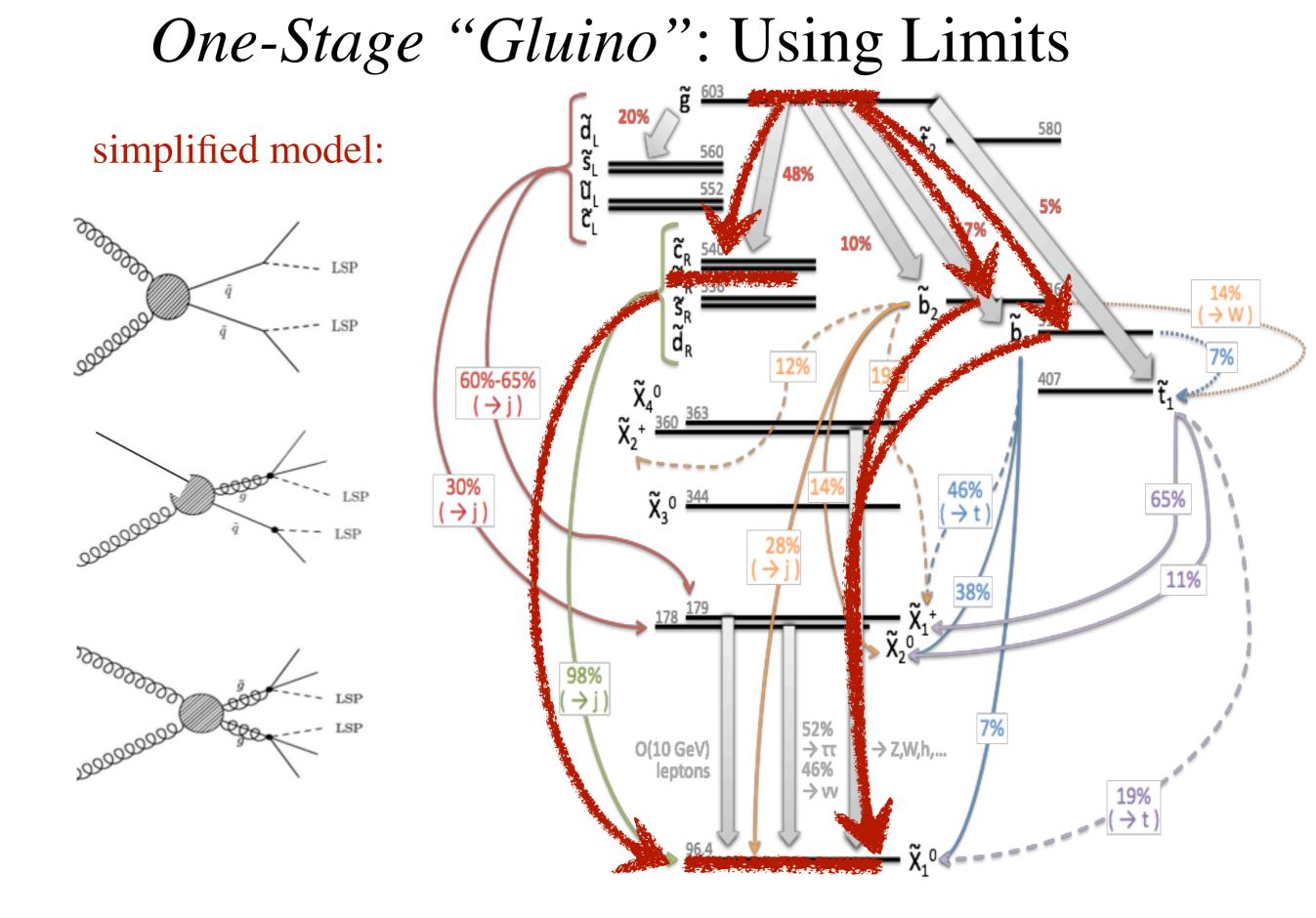
$$\sigma_{\max}(\mathcal{A}) = \frac{N_{\max}}{(\varepsilon_{\mathcal{A}} \times \mathcal{L})}$$

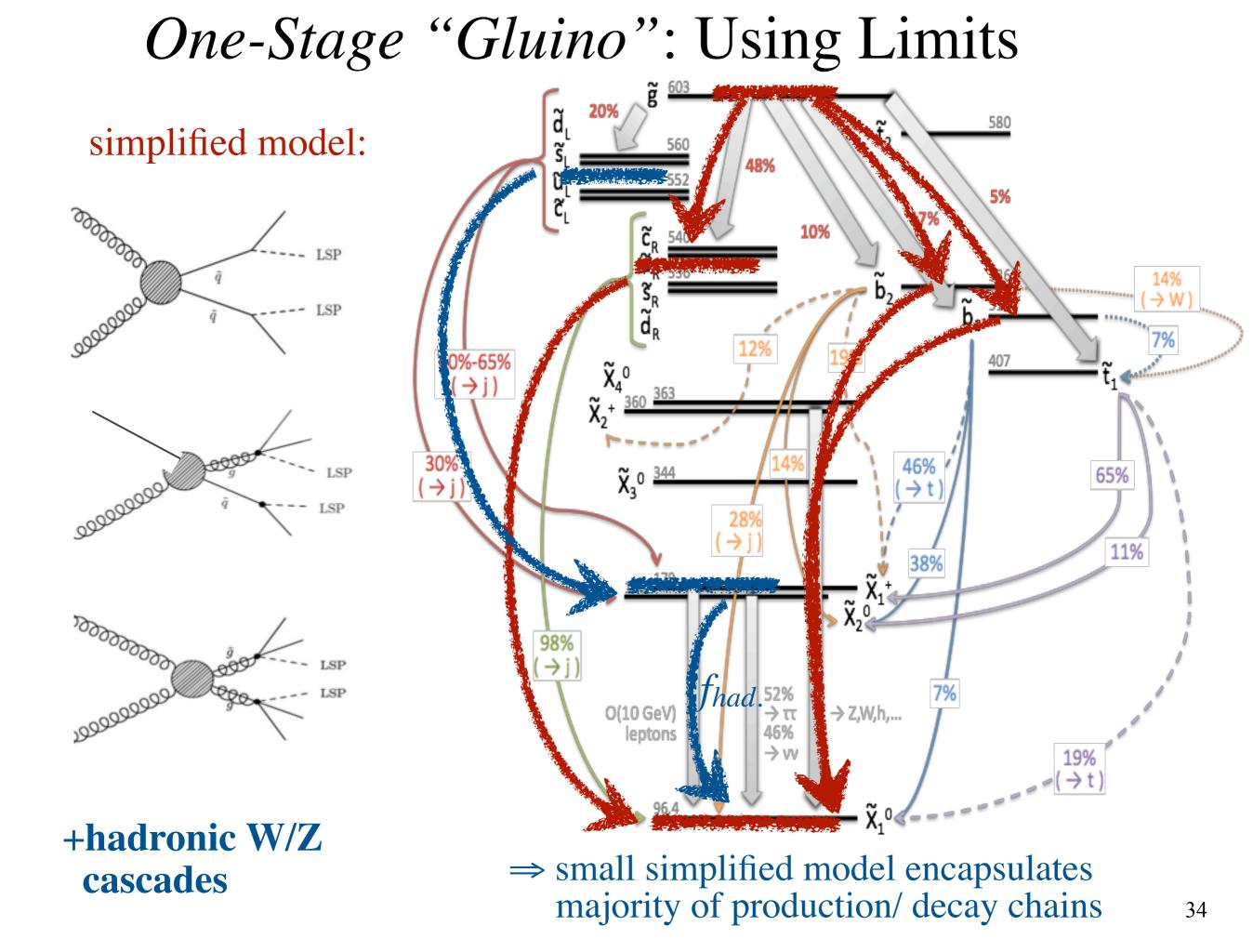
2) Calculate branching ratios for each process

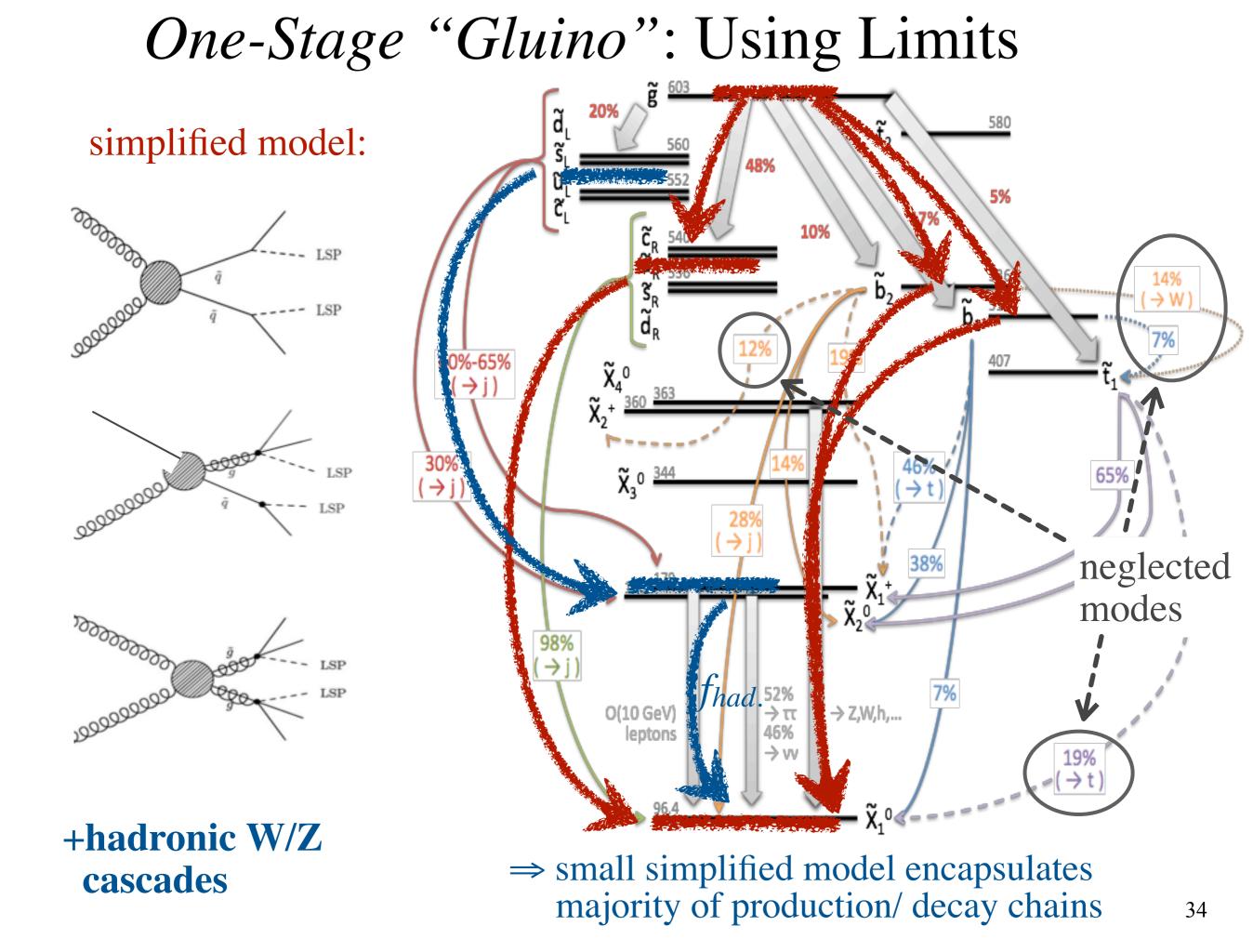
Require
$$\sum_{XY\to\mathcal{A}} \sigma_{XY} \times \mathcal{B}_{\mathcal{A}} \times \frac{1}{\sigma_{\max}(\mathcal{A})} < 1$$

Simple: take strongest limit among different search channels (*More sophisticated: combine likelihoods...eventually?*)

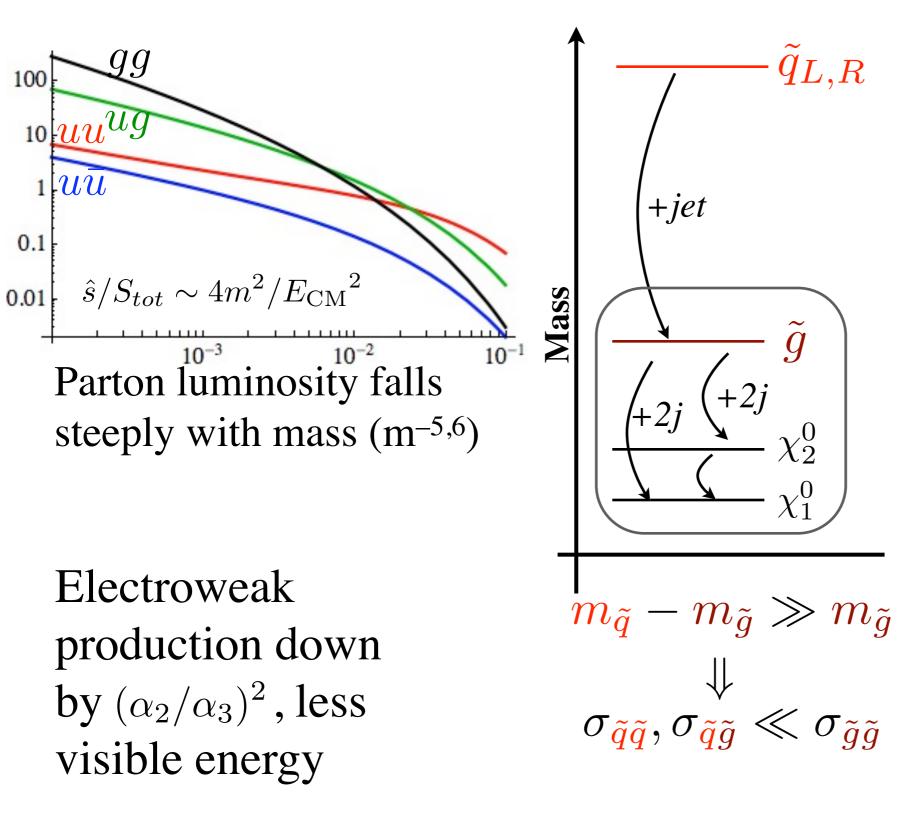








Theoretical Simplification: Production

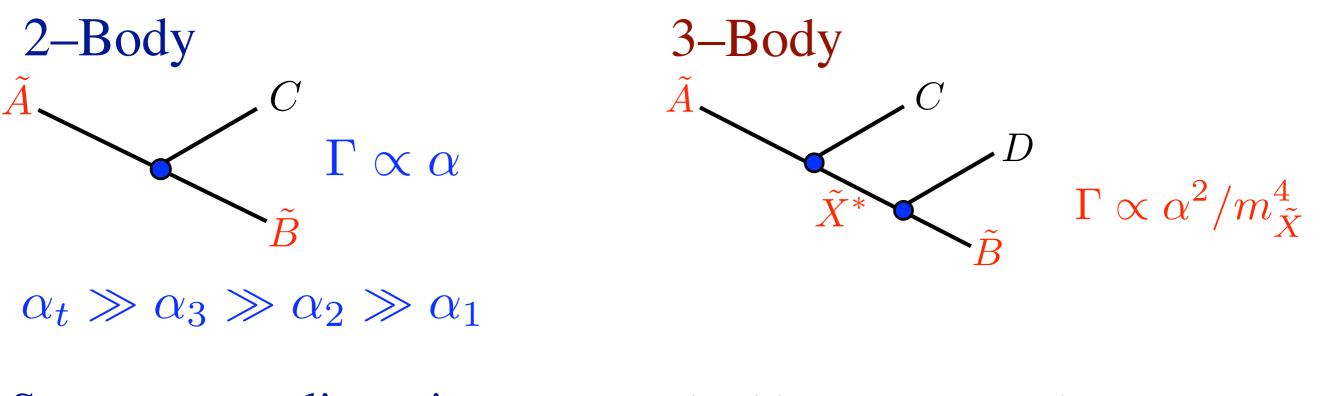


Mostly produce lightest (few) colored states

Theoretical Simplification: Decay

Feynman rules determined by Standard Model

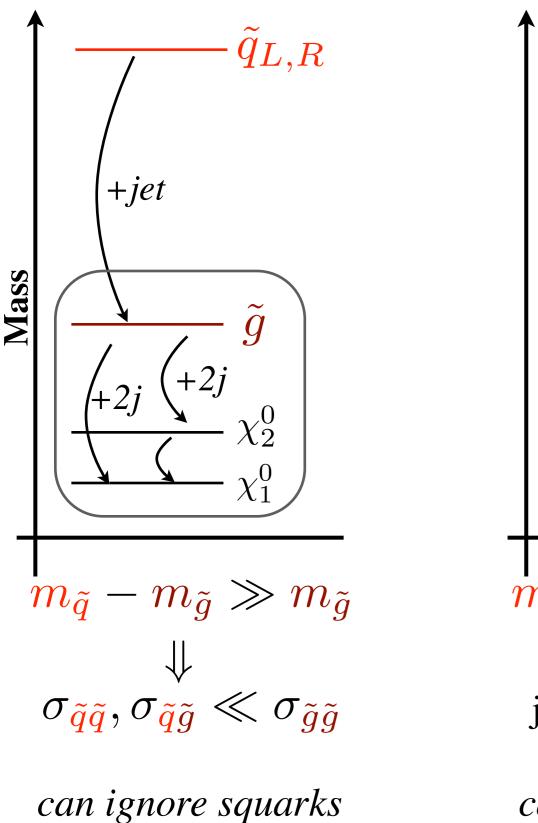
2-body decays dominate over 3-body, if allowed. (additional coupling & phase space suppression)



Strongest coupling wins

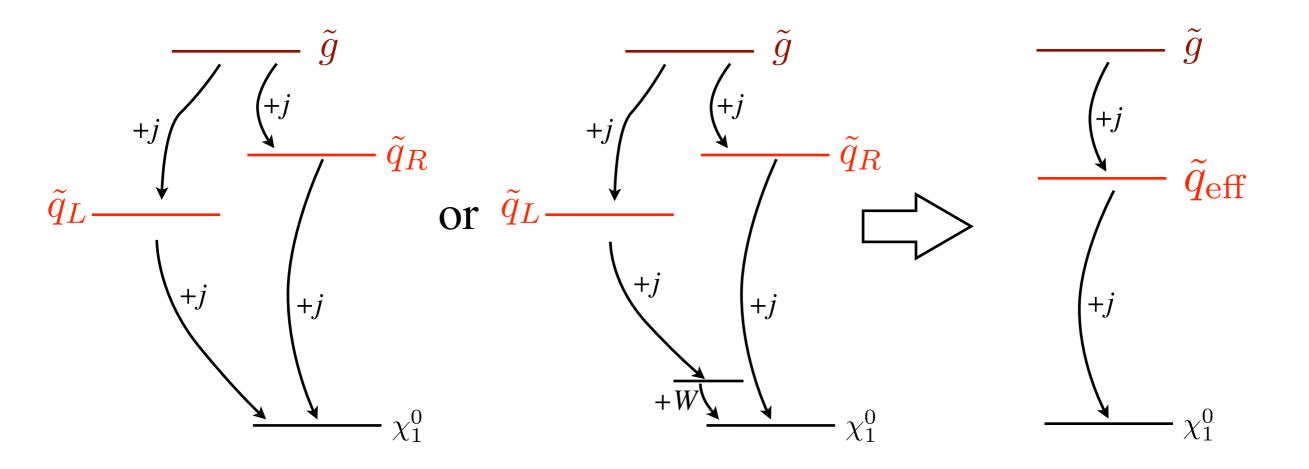
Significant suppression by couplings **and** intermediate mass

Experimental Simplification: Production



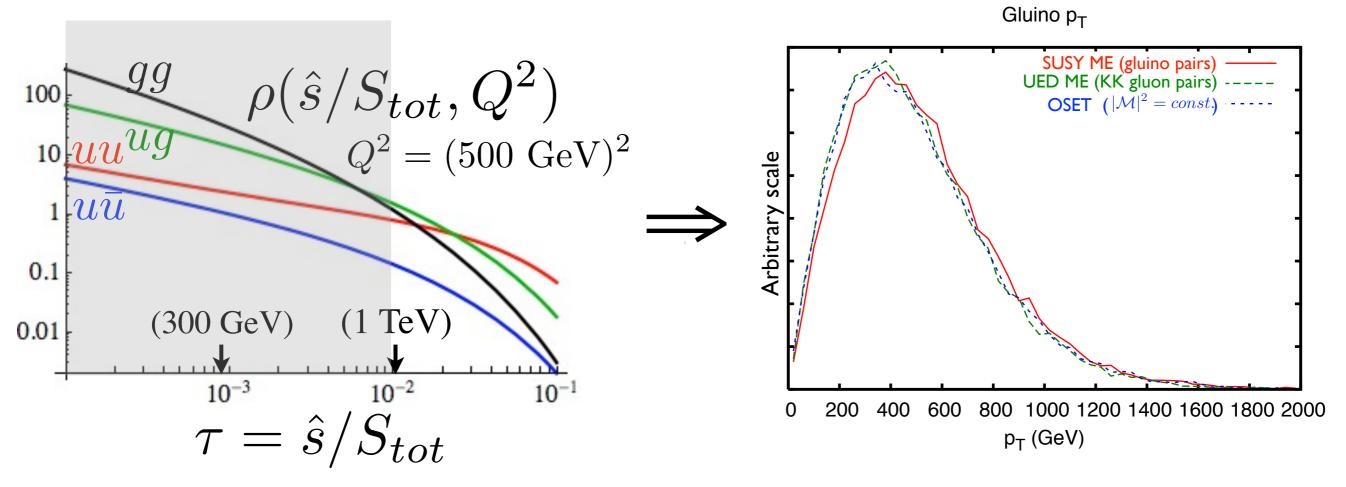
 $q_{L,R}$ +jet +2j χ^0_2 χ_1^0 $m_{\tilde{q}} - m_{\tilde{q}} \ll m_{\tilde{q}}$ jet from squark decay very soft can ignore squarks

Experimental Simplification: Decay



Similar intermediate states can be grouped together

Shape Invariance

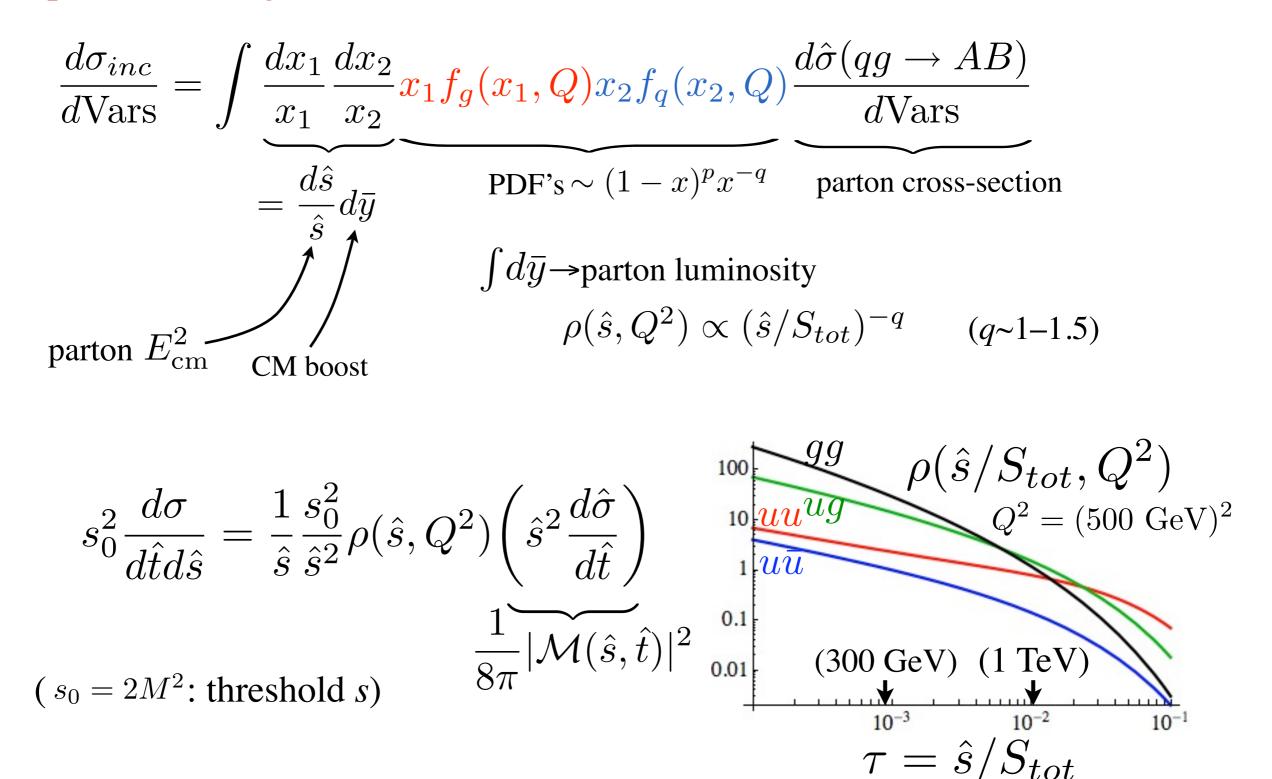


Final-state kinematics is *mostly* insensitive to the production matrix element.

This can be **justified analytically** (for object p_T 's and rapidity) by approximating parton luminosities near threshold as a power-law.

Remaining dependence can be parametrized simply, and/or absorbed in a bias of the "masses" used to characterize data.

Simple and instructive to calculate p_T distribution for $2\rightarrow 2$ product with general matrix element:



$$s_0^2 rac{d\sigma}{d\hat{t}d\hat{s}} = -rac{1}{\hat{s}} \; rac{s_0^2}{s^2}
ho(\hat{s},Q^2) |\mathcal{M}|^2 \quad
ho(\hat{s},s_0) pprox A(\hat{s}/S_{tot})^{-q}$$

CM-frame Lorentz invariants: $\hat{s} \& \hat{t}$ or $\hat{s} \& p_T^2$ or $\hat{s} \& \xi$

related by:
$$\hat{t} = -\frac{1}{2} \left[\hat{s}(1-\xi) - s_0 \right]$$
 $p_T^2 = \frac{\hat{t}\hat{u} - M^4}{\hat{s}} \Rightarrow dp_T^2 d\hat{s} = \xi d\hat{t} d\hat{s}$
 $\xi \sim \beta \cos \theta_{CM}$: "pure angular" variable linearly related to
 \Rightarrow good variable for M.E. expansion

$$s_0^2 rac{d\sigma}{dp_T^2} = rac{1}{\xi} \int\limits_{s_0+4p_T^2}^{S_{tot}} s_0^2 rac{d\sigma}{d\hat{t}d\hat{s}} = \int\limits_{s_0+4p_T^2}^{S_{tot}} rac{d\hat{s}}{\hat{s}} rac{s_0^2}{s^2}
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 \Rightarrow good variable for M.E. expansion

Expand $|\mathcal{M}|^2 = \sum C_{m,n} (\hat{s}/s_0)^m \xi^n$ near threshold (usually dominated by low m, n) $s_0^2 \frac{d\sigma}{dp_T^2} = \left(\frac{s_0}{S_{tot}}\right)^{-q} \sum_{m,n} C_{m,n} \int_{s_0+4p_T^2}^{S_{tot}} \frac{d\hat{s}}{\xi\hat{s}} (\hat{s}/s_0)^{m-q-2} \xi^n$

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$$s_0^2 rac{d\sigma}{dp_T^2} = rac{1}{\xi} \int\limits_{s_0+4p_T^2}^{S_{tot}} s_0^2 rac{d\sigma}{d\hat{t}d\hat{s}} = \int\limits_{s_0+4p_T^2}^{S_{tot}} rac{d\hat{s}}{\hat{s}} rac{s_0^2}{s^2}
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p_T Universality

pT variables are useful because they are simple, single-particle Lorentz invariants *and* insensitive to production matrix element!

 $\frac{d\sigma}{dp_T^2} \sim (1 + p_T^2/M^2)^{m-q-2} \quad \text{for} \quad |\mathcal{M}|^2 \sim (\hat{s}/s_0)^m \xi^n, \ \rho(\hat{s}) \sim \hat{s}^{-q}$ Typical p_T~0.5 M

- Not *completely* universal
 - Depends on *m* (different for p-wave and contact operators)
 - Depends on q (sensitive to init. state)
 - Observable p_T 's depend on decay M.E.
- **But** easy to get similar effects (after cuts) by changing s_0 simple analysis can't distinguish
- Similarly, η distribution indep. of m even different n convolved with \overline{y} distribution have similar shape

"Shape invariance" Arkani-Hamed et al, hep-ph/0703....